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AMERICAN MATHEMATICAL SOCIETY

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This journal is the official organ of the Society. It reports official acts of the Society and details of its meetings. It contains some of the officially invited addresses presented before the Society, research announcements and problems, and reviews of advanced mathematical books.

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Mathematical Reviews

This journal contains abstracts and reviews of the current mathematical literature of the world. It is sponsored by thirteen mathematical organizations, located both in the United States and abroad.

The publication of MATHEMATICAL REVIEWS was begun in 1940. Starting in 1961, it appears monthly, in two parts. Prior to 1961 it appeared in eleven single issues. Orders for complete volumes only are accepted. The price per volume is $50.00 except volumes 1–17 (1940–1956) which are available at $42.00 per volume. In 1962, it will be published in two volumes; the price of each volume will be $50.00.

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Notices of the American Mathematical Society

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Mathematics of Computation

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