

PROCEEDINGS
OF THE
AMERICAN MATHEMATICAL SOCIETY

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This is a cover to cover translation into English of Acta Mathematica Sinica, published by Academia Sinica Peking, People's Republic of China. Acta Mathematica Sinica contains current research in all fields of pure mathematics. Two volumes, Vols. 2 and 3, are planned for 1963. Vol. 1 (1962) \$30.00. Subscription price per volume is \$20.00.

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