## PROCEEDINGS

OF THE

# American Mathematical Society 

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## Proceedings of the American Mathematical Society

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