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LEE A. RUBEL
GEORGE B. SELIGMAN

WITH THE COOPERATION OF

Jay R. Goldman
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## AMS (MOS) MAJOR SUBJECT HEADINGS (1970)

The letters in parentheses indicate groupings which are used in the table of contents of each issue and in the volume index.

00 (H) General
01 (H) History and Biography
02 (E) Logic and Foundations
04 (E) Set Theory
05 (A) Combinatorics
06 (A) Order, Lattices, Ordered Algebraic Structures
08 (A) General Mathematical Systems
10 (A) Number Theory
12 (A) Algebraic Number Theory, Field Theory and Polynomials
13 (A) Commutative Rings and Algebras
14 (A) Algebraic Geometry
15 (A) Linear and Multilinear Algebra, Matrix Theory (finite and infinite)
16 (A) Associative Rings and Algebras
17 (A) Nonassociative Rings and Algebras
18 (A) Category Theory, Homological Algebra
20 (A) Group Theory and Generalizations
22 (G) Topological Groups, Lie Groups
26 (B) Real Functions
28 (B) Measure and Integration
30 (B) Functions of a Complex Variable
31 (B) Potential Theory
32 (B) Several Complex Variables and Analytic Spaces
33 (B) Special Functions
34 (B) Ordinary Differential Equations
35 (B) Partial Differential Equations
39 (B) Finite Differences and Functional Equations
40 (B) Sequences, Series, Summability
41 (B) Approximations and Expansions
42 (B) Fourier Analysis
43 (B) Abstract Harmonic Analysis

44 (B) Integral Transforms, Operational Calculus
45 (B) Integral Equations
46 (B) Functional Analysis
47 (B) Operator Theory
49 (B) Calculus of Variations and Optimal Control
50 (D) Geometry
52 (D) Convex Sets and Geometric Inequalities
53 (D) Differential Geometry
54 (G) General Topology
55 (G) Algebraic Topology
57 (G) Manifolds and Cell Complexes
58 (G) Global Analysis, Analysis on Manifolds
60 (F) Probability Theory and Stochastic Processes
62 (F) Statistics
65 (C) Numerical Analysis
68 (C) Computer Science
70 (C) Mechanics of Particles and Systems
73 (C) Mechanics of Solids
76 (C) Fluid Mechanics
78 (C) Optics, Electromagnetic Theory
80 (C) Classical Thermodynamics, Heat Transfer
81 (C) Quantum Mechanics
82 (C) Statistical Physics, Structure of Matter
83 (C) Relativity
85 (C) Astronomy and Astrophysics
86 (C) Geophysics
90 (C) Economics, Operations Research, Programming, Games
92 (C) Biology and Behavioral Sciences
93 (C) Systems, Control
94 (C) Information and Communication, Circuits, Automata
96 (H) Mathematical Education, Elementary
97 (H) Mathematical Education, Secondary
98 (H) Mathematical Education, Collegiate

# INDEX TO VOLUME 34 

## SUBJECT INDEX

*Starred items are "Shorter Notes"

## A. Algebra and Number Theory

5. Combinatorics

Goldsmith, D. L. and Gioia, A. A. On a question of Erdös concerning cohesive basic sequences, 356.
Kronk, Hudson V. and White, Arthur T. A 4-color theorem for toroidal graphs, 83.

Ryser, H. J. A fundamental matrix equation for finite sets, 332.
06. Order, Lattices, Ordered Algebraic Structures

Chambless, Donald A. Representation of the projectable and strongly projectable hulls of a lattice-ordered group, 346.
Kolibiar, M. Distributive sublattices of a lattice, 359.
Lea, J. W., Jr. An embedding theorem for compact semilattices, 325.
Sichler, J. Nonconstant endomorphisms of lattices, 67.
Smith, Dorothy P. Meet-irreducible elements in implicative lattices, 57.
10. Number Theory

Nathanson, Melvyn B. Complementing sets of n-tuples of integers, 71.
Plotkin, Neal. The solvability of the equation $a x^{2}+b y^{2}=c$ in quadratic fields, 337.
Segal, S. L. On convolutions with the Möbius function, 365.
Suryanarayana, D. and Rao, R. Sita Rama Chandra. The number of square-full divisors of an integer, 79.
12. Algebraic Number Theory, Field Theory and Polynomials

Kovacic, J. An Eisenstein criterion for noncommutative polynomials, 25.
Plotkin, Neal. The solvability of the equation $a x^{2}+b y^{2}=c$ in quadratic fields, 337.
Warner, Hoyt D. Determination of quadratic extensions of linearly compact fields by norm groups, 1.
13. Commutative Rings and Algebras

Carson, Andrew B. Coherence of polynomial rings over semisimple algebraic algebras, 20.
Chung, I. Y. Derivation modules of free joins and m-adic completions of algebras, 49.

Heinzer, William and Ohm, Jack. On the noetherian-like rings of E. G. Evans, 73. Hochster, M. Nonuniqueness of coefficient rings in a polynomial ring, 81.
15. Linear and Multilinear Algebra; Matrix Theory (finite and infinite)

Beasley, LeRoy B. and Cummings, Larry. Permanent groups, 351.
London, David and Minc, Henryk. Eigenvalues of matrices with prescribed entries, 8.
Stallings, W. T. and Boullion, T. L. The pseudoinverse of an r-circulant matrix, 385.
16. Associative Rings and Algebras

Beachy, John A. A characterization of torsionfree modules over rings of quotients, 15.

Camillo, V. P. and Fuller, K. R. Balanced and QF-1 algebras, 373.
Carson, Andrew B. Coherence of polynomial rings over semisimple algebraic algebras, 20.

Fisher, Joe W. Nil subrings of endomorphism rings of modules, 75.
Klein, Abraham A. Involutorial division rings with arbitrary centers, 38.
Rutter, Edgar A., Jr. Torsion theories over semiperfect rings, 389.

## 17. Nonassociative Rings and Algebras

Coughlin, Raymond. Nil algebras satisfying an identity of degree three, 63.
18. Category Theory, Homological Algebra

Chapman, G. R. On the relative group cohomology ring, 43.
Sichler, J. Nonconstant endomorphisms of lattices, 67.
20. Group Theory and Generalizations

Anshel, Michael and Prener, Robert. On free products of finite abelian groups, 343.
Bandelow, Christoph. On closed additive semigroups in $E^{n}, 87$.
Birman, Joan S. A normal form in the homeotopy group of a surface of genus 2, with applications to 3-manifolds, 379.
Fields, K. L. On the conjugating representation of a finite group, 35.
Hurley, James F. Normality and terminality in the elementary subgroups of Steinberg groups over rings, 30.
Stitzinger, Ernest L. Errata for two papers of Stitzinger, 631.
Yen, Ti. Permutable pronormal subgroups, 340.

## B. Analysis

## 26. Real Functions

Drasin, David and Shea, Daniel F. Pólya peaks and the oscillation of positive functions, 403.
Gariepy, Ronald. Geöcze area and a convergence property, 469.
Schmeidler, David. On set correspondences into uniformly convex Banach spaces, 97.

Smith, A. The differentiability of Riemann's function, 463.
Wright, Fred M. and Klasi, Melvin L. On existence and a dominated convergence, theorem for weighted g-summability, 479.
28. Measure and Integration

Gariepy, Ronald. Geöcze area and a convergence property, 469.

* Novinger, W. P. Mean convergence in L ${ }^{p}$ spaces, 627.

Uhl, J. J., Jr. A characterization of strongly measurable Pettis integrable functions, 425.

Wright, Fred M. and Klasi, Melvin L. On existence and a dominated convergence theorem for weighted g-summability, 479.
30. Functions of a Complex Variable

Brown, Leon and Hansen, Lowell. A nonnormal outer function in $H^{p}, 175$.
McCarty, Carl P. and Tepper, David E. A note on the $2 / 3$ conjecture for starlike functions, 417.
Protas, David. On the accumulation of the zeros of a Blaschke product at a boundary point, 489.
Taylor, B. A. and Williams, D. L. Interpolation of ${ }^{l}{ }^{q}$ sequences by $H^{\nu}$ functions, 181. 31. Potential Theory

Adams, David R. Maximal operators and capacity, 152.
33. Special Functions

Ullman, J. L. The location of the zeros of the derivatives of Faber polynomials, 422.

## 34. Ordinary Differential Equations

Chow, Shui-Nee and Lasota, A. An implicit function theorem for nondifferentiable mappings, 141.

Chow, Shui-Nee and Wong, Pui-Kei. A norm condition for disconjugacy of complex differential systems, 147.
Grimmer, R. On nonoscillatory solutions of a nonlinear differential equation, 118.
Heidel, J. W. A counterexample in nonlinear boundary value problems, 133.
Kreith, Kurt. Comparison theorems for nonselfadjoint differential equations based on integral inequalities, 105.

* Kroopnick, Allan. Properties of solutions of differential equations of the form $y^{\prime \prime}+a(t) b(y)=0,319$.
Rollins, L. W. Criteria for discrete spectrum of singular selfadjoint differential operators, 195.
Sleeman, B. D. The two-parameter Sturm-Liouville problem for ordinary differential equations. II, 165.

39. Finite Differences and Functional Equations

Nathanson, Melvyn B. Shift dynamical systems over finite fields, 591.
40. Sequences, Series, Summability

Bazinet, J. and Siddiqi, J. A. On nonstrongly regular matrices, 428.

* Wilansky, Albert. Separable and reflexive spaces of bounded sequences, 314.

41. Approximations and Expansions

Braess, D. On topological properties of sets admitting varisolvent functions, 453.
42. Fourier Analysis

Adams, David. Maximal operators and capacity, 152.
Benke, George. Arithmetic structure and lacunary Fourier series, 128.
Liu, Fon-che. On the localization of rectangular partial sums for multiple Fourier series, 90.
43. Abstract Harmonic Analysis

Benke, George. Arithmetic structure and lacunary Fourier series, 128.
Dunkl, Charles F. and Ramirez, Donald E. L ${ }^{p}$-convolution operators supported by subgroups, 475.
Lipsman, Ronald L. Equivalent conditions for the $L_{p}$ convolution theorem on semisimple groups, 497.
45. Integral Equations

Marrah, G. W. and Proctor, T. G. Solutions of some periodic Stieltjes integral equations, 121.

## 46. Functional Analysis

Baxley, John V. On the Weyl spectrum of a Hilbert space operator, 447.
Bouldin, Richard. Numerical range for certain classes of operators, 203.
Braun, Ben-Ami. An extension of a result by Talalyan on the representation of measurable functions by Schauder bases, 440.
Ching, Wai-mee and Willig, Paul. Nonasymptotically abelian factors of type III, 102.

Howe, Roger. The Brauer group of a compact Hausdorff space and n-homogeneous $C^{*}$-algebras, 209.
Husain, T. and Wong, Pak-Ken. On modular complemented and annihilator algebras, 457.

* Laursen, Kjeld B. Equivalence of algebra norms on $C(G), 316$.
* Lohman, Robert H. Isomorphisms in subspaces of $l_{1}, 323$.

Nakano, Hidegoro. On semicontinuous linear lattices, 115.

* Novinger, W. P. Mean convergence in $L^{p}$ spaces, 627.

Paschke, W. L. Completely positive maps on $U^{*}$-algebras, 412.
Roth, B. Finitely generated submodules of differentiable functions, 433.

Ruckle, William H. Reflexivity of $L(E, F), 171$.
Saxon, Stephen A. Embedding nuclear spaces in products of an arbitrary Banach space, 138.
Sundaresan, K. Orthogonality and nonlinear functionals on Banach spaces, 187.

* Wilansky, Albert. Separable and reflexive spaces of bounded sequences, 314.
——. Erratum to "Subalgebras of $B(X)$ ", 632.


## 47. Operator Theory

Baxley, John V. On the Weyl spectrum of a Hilbert space operator, 447.
Bouldin, Richard. Numerical range for certain classes of operators, 203.
Campbell, Stephen L. Linear operators for which $T^{*} T$ and $T T^{*}$ commute, 177.
Goor, Robert. On Toeplitz operators which are contractions, 191.
Guseman, L. F., Jr. and Solomon, J. L. Subsequential limit points of successive approximations, 573.
Horowitz, S. On finite invariant measures for sets of Markov operators, 110.
Ito, Takashi and Wong, Tin Kin. Subnormality and quasinormality of Toeplitz operators, 157.
Johnson, Gordon G. Fixed points by mean value iterations, 193.
Kalisch, Gerhard K. On operators on separable Banach spaces with arbitrary prescribed point spectrum, 207.
Ramanujan, P. B. and Patel, S. M. Erratum to "Operators whose ascent is 0 or 1", 632.

Randke, Daniel J. A factorization theorem for compact operators, 201.
Rollins, L. W. Criteria for discrete spectrum of singular selfadjoint differential operators, 195.
Wilansky, Albert. Erratum to "Subalgebras of $B(X)$ ", 632.
49. Calculus of Variations and Optimal Control

Tromba, A. J. The Morse lemma on Banach spaces, 396.

## D. Geometry

## 50. Geometry

Bandelow, Christoph. On closed additive semigroups in $E^{n}, 87$.

* Simmons, G. J. A quadrilateral-free arrangement of sixteen lines, 317.

52. Convex Sets and Geometric Inequalities

Lawrence, J. F., Hare, W. R., Jr. and Kenelly, John W. Finite unions of convex sets, 225.
Stavrakas, Nick M. The dimension of the convex kernel and points of local nonconvexity, 222.
Valentine, J. E. and Wayment, S. G. The euclidean symmetric isoceles queasy four-point properties, 233.
Zaks, Joseph. On a conjecture of A. J. Hoffman. II, 215.
53. Differential Geometry

Chen, Bang-yen. Minimal surfaces with constant Gauss curvature, 504.
Moore, John Douglas. Reducibility of isometric immersions, 229.
Wong, Yung-chow. On an explicit characterization of spherical curves, 239.

## E. Logic and Foundations

## 02. Logic and Foundations

Ellentuck, Erik and Rucker, R. V. B. Martin's axiom and saturated models, 243.
Shelah, Saharon. A note on model complete models and generic models, 509.

## F. Statistics and Probability

## 60. Probability Theory and Stochastic Processes

Isaacson, Dean. On a subclass of square integrable martingales, 521.
Woyczyński, W. A. Linear processes generated by independent random variables, 515.

G. TÓPology

## 22. Topological Groups, Lie Groups

Lea, J. W., Jr. An embedding theorem for compact semilattices, 325.
Lee, D. H. Group extensions and discrete subgroups of Lie groups, 299.
Morris, Sidney A. Locally compact abelian groups and the variety of topological groups generated by the reals, 290.
Neuberger, J. W. Differentiable semigroups with a neighborhood of the identity homeomorphic to a Banach space, 595.
Sharpe, Kevin J. Two properties of $R^{N}$ with a compact group topology, 267.

## 54. General Topology

Bonnett, Dennis A. A symmetrizable space that is not perfect, 560.
Dooley, Robert A. Extending a complete convex metric, 553.
Enos, H. C. Coarse uniformities on the rationals, 623.
Guseman, L. F., Jr. and Solomon, J. L. Subsequential limit points of successive approximations, 573.
Harley, P. W. III. A characterization of spaces on which all path maps are continuous, 621.
Hass, Dennis C. Recognizing manifolds among generalized manifolds, 311.
Lea, J. W., Jr. An embedding theorem for compact semilattices, 325.
Proctor, C. Wayne. A characterization of hereditrarily indecomposable continua, 287.

Sharma, P. L. Lattice-invariant topological properties, 565.
Stephenson, R. M., Jr. Discrete subsets of perfectly normal spaces, 605.
Thornton, Melvin C. Semirings of functions determine finite $T_{0}$ topologies, 307.
Treybig, L. B. Local degree of separability and invariance of domain, 273.
Wagner, Neal R. The space of retractions of a 2-manifold, 609.

## 55. Algebraic Topology

Birman, Joan S. A normal form in the homeotopy group of a surface of genus 2, with applications to 3-manifolds, 379.
Chen, Kuo-Tsai. On Whitehead products, 257.
Kim, Soon-kyu. Local triviality of fiberings, 546.
McAuley, Patricia Tulley. A note on paired fibrations, 534.
Mukherjea, Kalyan K. New methods in coincidence theory, 615.
Nomura, Yasutoshi. Homology of a fibration over an aspherical space, 527.
Parks, James M. Applications of homotopy in sheaf theory, 601.
Shar, Albert. $\pi_{m n-2}\left(S_{m-2}^{n}\right)$ contains an element of order $m, 303$.
Sternstein, Martin. Necessary and sufficient conditions for homotopy classification by cohomology and homotopy homomorphisms, 250.
Whitten, Wilbur. Fibered knots through T-surgery, 293.

## 57. Manifolds and Cell Complexes

Cutler, William H. Deficiency in F-manifolds, 260.
Daverman, Robert J. Wild cells in $E^{4}$ in which every arc is tame, 270.
Heil, Wolfgang. On certain fiberings of $M^{2} \times S^{1}, 280$.
Lawson, Terry C. Some examples of nonfinite diffeomorphism groups, 570.

Parker, George D. Morse theory on Kähler homogeneous spaces, 586.
Row, W. H., Jr. Irreducible 3-manifolds whose orientable covers are not prime, 541.
Wagner, Neal R. The space of retractions of a 2-manifold, 609.
58. Global Analysis, Analysis on Manifolds

Cutler, William H. Deficiency in F-manifolds, 260.

* England, James W. The zeta function of toral endomorphisms, 321.

Nathanson, Melvyn B. Shift dynamical systems over finite fields, 591.

* Simon, Carl P. A 3-dimensional Abraham-Smale example, 629.

Tromba, A. J. Some theorems on Fredholm maps, 578.

# AUTHOR INDEX 

*Starred items are "Shorter Notes"

Adams, David R. Maximal operators and capacity, 152.
Anshel, Michael and Prener, Robert. On free products of finite abelian groups, 343.
Bandelow, Christoph. On closed additive semigroups in $E^{n}, 87$.
Baxley, John V. On the Weyl spectrum of a Hilbert space operator, 447.
Bazinet, J. and Siddiqi, J. A. On nonstrongly regular matrices, 428.
Beachy, John A. A characterization of torsionfree modules over rings of quotients, 15.
Beasley, LeRoy B. and Cummings, Larry. Permanent groups, 351.
Benke, George. Arithmetic structure and lacunary Fourier series, 128.
Birman, Joan S. A normal form in the homeotopy group of a surface of genus 2 , with applications to 3-manifolds, 379.
Bonnett, Dennis A. A symmetrizable space that is not perfect, 560 .
Bouldin, Richard. Numerical range for certain classes of operators, 203.
Boullion, T. L. See Stallings, W. T.
Braess, D. On topological properties of sets admitting varisolvent functions, 453.
Braun, Ben-Ami. An extension of a result of Talalyan on the representation of measurable functions by Schauder bases, 440.
Brown, Leon and Hansen, Lowell. A nonnormal outer function in $H^{p}, 175$.
Camillo, V. P. and Fuller, K. R. Balanced and QF-1 algebras, 373.
Campbell, Stephen L. Linear operators for which T*T and TT* commute, 177.
Carson, Andrew B. Coherence of polynomial rings over semisimple algebraic algebras, 20.
Chambless, Donald A. Representation of the projectable and strongly projectable hulls of a lattice-ordered group, 346.
Chapman, G. R. On the relative group cohomology ring, 43.
Chen, Bang-yen. Minimal surfaces with constant Gauss curvature, 504.
Chen, Kuo-Tsai. On Whitehead products, 257.
Ching, Wai-mee and Willig, Paul. Nonasymptotically abelian factors of type III, 102.
Chow, Shui-Nee and Lasota, A. An implicit function theorem for nondifferentiable mappings, 141.
Chow, Shui-Nee and Wong, Pui-Kei. A norm condition for disconjugacy of complex differential systems, 147.
Chung, I. Y. Derivation modules of free joins and $\mathfrak{m}$-adic completions of algebras, 49.
Coughlin, Raymond. Nil algebras satisfying an identity of degree three, 63.
Cummings, Larry. See Beasley, LeRoy B.
Cutler, William H. Deficiency in F-manifolds, 260.
Daverman, Robert J. Wild cells in $E^{4}$ in which every arc is tame, 270.
Dooley, Robert A. Extending a complete convex metric, 553.
Drasin, David and Shea, Daniel F. Pólya peaks and the oscillation of positive functions, 403.

Dunkl, Charles F. and Ramirez, Donald E. $L^{p}$-Convolution operators supported by subgroups, 475.
Ellentuck, Erik and Rucker, R.V.B. Martin's axiom and saturated models, 243.

* England, James W. The zeta function of toral endomorphisms, 321.

Enos, H. C. Coarse uniformities on the rationals, 623.
Fields, K. L. On the conjugating representation of a finite group, 35.

Fisher, Joe W. Nil subrings of endomorphism rings of modules, 75.
Fuller, K. R. See Camillo, V. P.
Gariepy, Ronald. Geöcze area and a convergence property, 469.
Gioia, A. A. See Goldsmith, D. L.
Goldsmith, D. L. and Gioia, A. A. On a question of Erdös concerning cohesive basic sequences, 356.
Goor, Robert. On Toeplitz operators which are contractions, 191.
Grimmer, R. On nonoscillatory solutions of a nonlinear differential equation, 118.
Guseman, L. F., Jr. and Solomon, J. L. Subsequential limit points of successive approximations, 573.
Hansen, Lowell. See Brown, Leon.
Hare, W. R., Jr. See Lawrence, J. F.
Harley, P. W. III. A characterization of spaces on which all path maps are continuous, 621.
Hass, Dennis C. Recognizing manifolds among generalized manifolds, 311.
Heidel, J. W. A counterexample in nonlinear boundary value problems, 133.
Heil, Wolfgang. On certain fiberings of $M^{2} \times S^{1}, 280$.
Heinzer, William and Ohm, Jack. On the noetherian-like rings of E. G. Evans, 73.
Hochster, M. Nonuniqueness of coefficient rings in a polynomial ring, 81.
Horowitz, S. On finite invariant measures for sets of Markov operators, 110.
Howe, Roger. The Brauer group of a compact Hausdorff space and n-homogeneous $C^{*}$-algebras, 209.
Hurley, James F. Normality and terminality in the elementary subgroups of Steinberg groups over rings, 30.
Husain, T. and Wong, Pak-Ken. On modular complemented and annihilator algebras, 457.

Isaacson, Dean. On a subclass of square integrable martingales, 521.
Ito, Takashi and Wong, Tin Kin. Subnormality and quasinormality of Toeplitz operators, 157.

Johnson, Gordon G. Fixed points by mean value iterations, 193.
Kalisch, Gerhard K. On operators on separable Banach spaces with arbitrary prescribed point spectrum, 207.
Kenelly, John W. See Lawrence, J. F.
Kim, Soon-kyu. Local triviality of fiberings, 546.
Klasi, Melvin L. See Wright, Fred M.
Klein, Abraham A. Involutorial division rings with arbitrary centers, 38.
Kolibiar, M. Distributive sublattices of a lattice, 359.
Kovacic, J. An Eisenstein criterion for noncommutative polynomials, 25.
Kreith, Kurt. Comparison theorems for nonselfadjoint differential equations based on integral inequalities, 105.
Kronk, Hudson V. and White, Arthur T. A 4-color theorem for toroidal graphs, 83.

* Kroopnick, Allan. Properties of solutions of differential equations of the form $y^{\prime \prime}+a(t) b(y)=0,319$.
Lasota, A. See Chow, Shui-Nee.
* Laursen, Kjeld B. Equivalence of algebra norms on $C(G), 316$.

Lawrence, J. F., Hare, W. R., Jr. and Kenelly, John W. Finite unions of convex sets, 225. Lawson, Terry C. Some examples of nonfinite diffeomorphism groups, 570.
Lea, J. W., Jr. An embedding theorem for compect semilattices, 325.
Lee, D. H. Group extensions and discrete subgroups of Lie groups, 299.
Lipsman, Ronald L. Equivalent conditions for the $L_{p}$ convolution theorem on semisimple groups, 497.

Liu, Fon-che. On the localization of rectangular partial sums for multiple Fourier series 90.

* Lohman, Robert H. Isomorphisms in subspaces of $l_{1}, 323$.

London, David and Minc, Henryk. Eigenvalues of matrices with prescribed entries, 8.
McAuley, Patricia Tulley. A note on paired fibrations, 534.
McCarty, Carl P. and Tepper, David E. A note on the $2 / 3$ conjecture for starlike functions, 417.

Marrah, G. W. and Proctor, T. G. Solutions of some periodic Stieltjes integral equations, 121.

Minc, Henryk. See London, David.
Moore, John Douglas. Reducibility of isometric immersions, 229.
Morris, Sidney A. Locally compact abelian groups and the variety of topological groups generated by the reals, 290.
Mukherjea, Kalyan K. New methods in coincidence theory, 615.
Nakano, Hidegoro. On semicontinuous linear lattices, 115.
Nathanson, Melvyn B. Complementing sets of $n$-tuples of integers, 71.
——. Shift dynamical systems over finite fields, 591.
Neuberger, J. W. Differentiable semigroups with a neighborhood of the identity homeomorphic to a Banach space, 595.
Nomura, Yasutoshi. Homology of a fibration over an aspherical space, 527.

* Novinger, W. P. Mean convergence in $L^{p}$ spaces, 627.

Ohm, Jack. See Heinzer, William.
Parker, George D. Morse theory on Kähler homogeneous spaces, 586.
Parks, James M. Applications of homotopy in sheaf theory, 601.
Paschke, W. L. Completely positive maps on $U^{*}$-algebras, 412.
Patel, S. M. See Ramanujan, P. B.
Plotkin, Neal. The solvability of the equation $a x^{2}+b y^{2}=c$ in quadratic fields, 337.
Prener, Robert. See Anshel, Michael.
Proctor, C. Wayne. A characterization of hereditarily indecomposable continua, 287.
Proctor, T. G. See Marrah, G. W.
Protas, David. On the accumulation of the zeros of a Blaschke product at a boundary point, 489.
Ramanujan, P. B. and Patel, S. M. Erratum to "Operators whose ascent is 0 or 1", 632.
Ramirez, Donald E. See Dunkl, Charles F.
Randtke, Daniel J. A factorization theorem for compact operators, 201.
Rao, R. Sita Rama Chandra. See Suryanarayana, D.
Rollins, L. W. Criteria for discrete spectrum of singular selfadjoint differential operators, 195.

Roth, B. Finitely generated submodules of differentiable functions, 433.
Row, W. H., Jr. Irreducible 3-manifolds whose orientable covers are not prime, 541.
Ruckle, William H. Reflexivity of $L(E, F), 171$.
Rucker, R. V. B. See Ellentuck, Erik.
Rutter, Edgar A., Jr. Torsion theories over semiperfect rings, 389.
Ryser, H. J. A fundamental matrix equation for finite sets, 332.
Saxon, Stephen A. Embedding nuclear spaces in products of an arbitrary Banach space, 138.
Schmeidler, David. On set correspondences into uniformly convex Banach spaces, 97.
Segal, S. L. On convolutions with the Möbius functions, 365.
Shar, Albert. $\pi_{m n-2}\left(S_{m-2}^{n}\right)$ contains an element of order $m, 303$.
Sharma, P. L. Lattice-invariant topological properties, 565.
Sharpe, Kevin J. Two properties of $R^{\mathcal{N}}$ with a compact group topology, 267.
Shea, Daniel F. See Drasin, David.

Shelah, Saharon. A note on model complete models and generic models, 509.
Sichler, J. Nonconstant endomorphisms of lattices, 67.
Siddiqi, J. A. See Bazinet, J.

* Simmons, G. J. A quadrilateral-free arrangement of sixteen lines, 317.
* Simon, Carl P. A 3-dimensional Abraham-Smale example, 629.

Sleeman, B. D. The two-parameter Sturm-Liouville problem for ordinary differential equations. II, 165.
Smith, A. The differentiability of Riemann's function, 463.
Smith, Dorothy P. Meet-irreducible elements in implicative lattices, 57.
Solomon, J. L. See Guseman, L. F., Jr.
Stallings, W. T. and Boullion, T. L. The pseudoinverse of an r-circulant matrix, 385.
Stavrakas, Nick M. The dimension of the convex kernel and points of local nonconvexity, 222.

Stephenson, R. M., Jr. Discrete subsets of perfectly normal spaces, 605.
Sternstein, Martin. Necessary and sufficient conditions for homotopy classification by cohomology and homotopy homomorphisms, 250.
Stitzinger, Ernest L. Errata for two papers of Stitzinger, 631.
Sundaresan, K. Orthogonality and nonlinear functionals on Banach spaces, 187.
Suryanarayana, D. and Rao, R. Sita Rama Chandra. The number of square-full divisors of an integer, 79.
Taylor, B. A. and Williams, D. L. Interpolation of $l^{l}$ sequences by $H^{p}$ functions, 181. Tepper, David E. See McCarty, Carl P.
Thornton, Melvin C. Semirings of functions determine finite $T_{0}$ topologies, 307.
Treybig, L. B. Local degree of separability and invariance of domain, 273.
Tromba, A. J. The Morse lemma on Banach spaces, 396.
—_. Some theorems on Fredholm maps, 578.
Uhl, J. J., Jr. A characterization of strongly measurable Pettis integrable functions, 425.
Ullman, J. L. The location of the zeros of the derivatives of Faber polynomials, 422.
Valentine, J. E. and Wayment, S. G. The euclidean symmetric isoceles queasy four-point properties, 233.
Wagner, Neal R. The space of retractions of a 2-manifold, 609.
Warner, Hoyt D. Determination of quadratic extensions of linearly compact fields by norm groups, 1.
Wayment, S. G. See Valentine, J. E.
White, Arthur T. See Kronk, Hudson V.
Whitten, Wilbur. Fibered knots through T-surgery, 293.

* Wilansky, Albert. Separable and reflexive spaces of bounded sequences, 314.
-. Erratum to "Subalgebras of $B(X)$ ", 632.
Williams, D. L. See Taylor, B. A.
Willig, Paul. See Ching, Wai-mee.
Woyczyński, W. A. Linear processes generated by independent random variables, 515.
Wong, Pak-Ken. See Husain, T.
Wong, Pui-Kei. See Chow, Shui-Nee.
Wong, Tin Kin. See Ito, Takashi.
Wong, Yung-chow. On an explicit characterization of spherical curves, 239.
Wright, Fred M. and Klasi, Melvin L. On existence and a dominated convergence theorem for weighted g-summability, 479.
Yen, Ti. Permutable pronormal subgroups, 340.
Zaks, Joseph. On a conjecture of A. J. Hoffman. II, 215.


## Contents-Continued from back cover

On the accumulation of the zeros of a Blaschke product at a boundary point. By David Protas ..... 489
Equivalent conditions for the $L_{p}$ convolution theorem on semisimple groups. By Ronald L. Lipsman ..... 497
D. Geometry
Minimal surfaces with constant Gauss curvature. By Bang-yen Chen ..... 504
E. Logic and Foundations
A note on model complete models and generic models. By Saharon Shelah ..... 509
F. Statistics and Probability
Linear processes generated by independent random variables. By W. A. WOYCZYŃSKI ..... 515
On a subclass of square integrable martingales. By Dean Isaacson ..... 521
G. Topology
Homology of a fibration over an aspherical space. By Yasutoshi Nomura ..... 527
A note on paired fibrations. By Patricia Tully McAuley ..... 534
Irreducible 3-manifolds whose orientable covers are not prime. By W. H. Row, Jr ..... 541
Local triviality of fiberings. By Soon-kyu Kim ..... 546
Extending a complete convex metric. By Robert A. Dooley ..... 553
A symmetrizable space that is not perfect. By Dennis A. Bonnett ..... 560
Lattice-invariant topological properties. By P. L. Sharma ..... 565
Some examples of nonfinite diffeomorphism groups. By Terry C. Lawson ..... 570
Subsequential limit points of successive approximations. By L. F. Guseman, Jr. and J. L. Solomon ..... 573
Some theorems on Fredholm maps. By A. J. Tromba ..... 578
Morse theory on Kähler homogeneous spaces. By George D. Parker ..... 586
Shift dynamical systems over finite fields. By Melvyn B. Nathanson ..... 591
Differentiable semigroups with a neighborhood of the identity homeomorphic to a Banach space. By J. W. Neuberger ..... 595
Applications of homotopy in sheaf theory. By James M. Parks ..... 601
Discrete subsets of perfectly normal spaces. By R. M. Stephenson, Jr. ..... 605
The space of retractions of a 2 -manifold. By Neal R. Wagner ..... 609
New methods in coincidence theory. By Kalyan K. Mukherjea ..... 615
A characterization of spaces on which all path maps are continuous. By P. W. Harley III ..... 621
Coarse uniformities on the rationals. By H. C. Enos ..... 623
Shorter Notes
Mean convergence in $L^{p}$ spaces. By W. P. Novinger ..... 627
A 3-dimensional Abraham-Smale example. By Carl P. Simon ..... 629
Errata for two papers of Stitzinger. By Ernest L. Stitzinger ..... 631
Errata to Volume 29 ..... 632
AMS (MOS) Major Subject Headings (1970) ..... 633
Index to Volume 34 ..... 635

## CONTENTS*

Vol. 34, No. 2 AUGUST 1972 Whole No. 158
Page
A. Algebra and Number Theory
An embedding theorem for compact semilattices. By J. W. Lea, Jr. ..... 325
A fundamental matrix equation for finite sets. By H. J. Ryser ..... 332
The solvability of the equation $a x^{2}+b y^{2}=c$ in quadratic fields. By Neal Plotkin ..... 337
Permutable pronormal subgroups. By Ti Yen ..... 340
On free products of finite abelian groups. By Michael Anshel and Robert Prener ..... 343
Representation of the projectable and strongly projectable hulls of a lattice- ordered group. By Donald A. Chambless ..... 346
Permanent groups. By LeRoy B. Beasley and Larry Cummings ..... 351
On a question of Erdös concerning cohesive basic sequences. By D. L. Goldsmith and A. A. Gioia ..... 356
Distributive sublattices of a lattice. By M. Kolibiar ..... 359
On convolutions with the Möbius function. By S. L. Segal ..... 365
Balanced and QF-1 algebras. By V. P. Camillo and K. R. Fuller ..... 373
A normal form in the homeotopy group of a surface of genus 2, with applications to 3-manifolds. By Joan S. Birman ..... 379
The pseudoinverse of an $r$-circulant matrix. By W. T. Stallings and T. L. Boullion ..... 385
Torsion theories over semiperfect rings. By Edgar A. Rutter, Jr. ..... 389
B. Analysis
The Morse lemma on Banach spaces. By A. J. Tromba ..... 396
Pólya peaks and the oscillation of positive functions. By David Drasin and Daniel F. Shea ..... 403
Completely positive maps on $U^{*}$-algebras. By W. L. Paschke ..... 412
A note on the $2 / 3$ conjecture for starlike functions. By Carl P. McCarty and David E. Tepper ..... 417
The location of the zeros of the derivatives of Faber polynomials. By J. L. Ullman ..... 422
A characterization of strongly measurable Pettis integrable functions. By J. J. UhL, JR. ..... 425
On nonstrongly regular matrices. By J. Bazinet and J. A. Siddiqi ..... 428
Finitely generated submodules of differentiable functions. By B. Rотн ..... 433
An extension of a result by Talalyan on the representation of measurable functions by Schauder bases. By Ben-Ami Braun ..... 440
On the Weyl spectrum of a Hilbert space operator. By John V. Baxley ..... 447
On topological properties of sets admitting varisolvent functions, By D. BraESS ..... 453
On modular complemented and annihilator algebras. By T. Husain and Pak-Ken Wong ..... 457
The differentiability of Riemann's function. By A. Smith ..... 463
Geöcze area and a convergence property. By Ronald Gariepy ..... 469
$L^{p}$-convolution operators supported by subgroups. By Charles F. Dunkl and Donald E. Ramirez ..... 475
On existence and a dominated convergence theorem for weighted $g$-summability. By Fred M. Wright and Melvin L. Klasi ..... 479

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[^0]:    * The volume index will contain a mapping showing the correspondence between sections A-G and the AMS (MOS) subject classification numbers.

