

PROCEEDINGS  
OF THE  
AMERICAN MATHEMATICAL SOCIETY

EDITED BY

FRED G. BRAUER	JACOB FELDMAN
GLEN E. BREDON	JOSEPH J. ROTMAN
W. WISTAR COMFORT	LEE A. RUBEL
GEORGE B. SELIGMAN	

WITH THE COOPERATION OF

JAY R. GOLDMAN	ALLEN L. SHIELDS
JAMES D. KUELBS	ROBERT I. SOARE

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## Proceedings of the American Mathematical Society

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# CONTENTS\*

Vol. 35, No. 1

SEPTEMBER 1972

Whole No. 159

	Page
A. ALGEBRA AND NUMBER THEORY	
The finiteness of $I$ when $R[X]/I$ is $R$ -flat. II. By WILLIAM HEINZER and JACK OHM	1
An application of the algebra of differentials of infinite rank. By WILLIAM C. BROWN	9
Quotient rings of endomorphism rings of modules with zero singular submodule. By JOHN HUTCHINSON and JULIUS ZELMANOWITZ	16
The probability of connectedness of an unlabelled graph can be less for more edges. By E. M. WRIGHT	21
On an induction theorem for relative Grothendieck groups. By WILLIAM H. GUSTAFSON	26
Isomorphism types of infinite symmetric graphs. By C. M. BANG	31
An improved upper bound for global dimension of semigroup algebras. By WILLIAM R. NICO	34
The epimorphic images of a Dedekind domain. By T. CHEATHAM and E. ENOCHS	37
Quasi-cotripleable categories. By ROBERT C. DAVIS	43
A counterexample to an analogue of Artin's conjecture. By P. J. WEINBERGER	49
Operators associated with a pair of nonnegative matrices. By GERALD E. SUCHAN	53
Ideals generated by three elements. By PETER KOHN	55
Zeros of $\zeta'(s)$ in the critical strip. By ROBERT SPIRA	59
A finitely presented metabelian group with a free abelian derived group of infinite rank. By GILBERT BAUMSLAG	61
Two observations on the congruence extension property. By G. GRÄTZER and H. LAKSER	63
Tensor products of quaternion algebras. By A. A. ALBERT	65
B. ANALYSIS	
Extremal problems for certain classes of analytic functions. By LOUIS BRICKMAN	67
The Fourier transform of an unbounded spectral distribution. By BRIAN KRITT	74
Noncoincidence of the strict and strong operator topologies. By JOEL H. SHAPIRO	81
On the range of a coercive maximal monotone operator in a nonreflexive Banach space. By JEAN-PIERRE GOSSEZ	88
Integral as a certain type of a positive definite function. By PARFENY P. SAWOROTNOW	93
A generalization of two inequalities involving means. By SCOTT LAWRENCE and DANIEL SEGALMAN	96
The numerical range of a Toeplitz operator. By E. M. KLEIN	101
Nonfactorization in subsets of the measure algebra. By J. T. BURNHAM	104
Perturbed asymptotically stable sets. By ROGER C. MCCANN	107
Total stability in nondifferentiable systems. By ROGER C. MCCANN	112
Second order almost linear functional differential equations—Oscillation. By HUGO TEUFEL, JR.	117
The existence of oscillatory solutions for the equation $d^2y/dt^2 + q(t)y' = 0$ , $0 < r < 1$ . By KUO-LIANG CHIOU	120
On the Laplace transform of a temperate distribution supported by a cone. By BENT E. PETERSEN	123
Existence of solutions of abstract measure differential equations. By R. R. SHARMA	129
On the length of gaps in the essential spectrum of a generalised Dirac operator. By W. D. EVANS	137
A random Trotter product formula. By THOMAS G. KURTZ	147

\* The volume indexes contain a mapping showing the correspondence between sections A–G and the AMS (MOS) subject classification numbers.

Boundary zero sets of $A^\infty$ functions satisfying growth conditions. By B. A. TAYLOR and D. L. WILLIAMS.....	155
Sparse subsets of orthonormal systems. By J. J. PRICE.....	161
A nonlinear complementarity problem in mathematical programming in Banach space. By M. S. BAZARAA, J. J. GOODE and M. Z. NASHED.....	165
A fixed point theorem for asymptotically nonexpansive mappings. By K. GOEBEL and W. A. KIRK.....	171
Nonexistence of asymptotic observables. By JAMES S. HOWLAND.....	175
On a general ratio ergodic theorem with weighted averages. By RYOTARO SATO.....	177
The Teichmüller spaces are distinct. By DAVID B. PATTERSON.....	179
Existence of a seminormal basis in $C[0, 1]$ . By SHERWOOD SAMN.....	183
Eventual disconjugacy of selfadjoint fourth order linear differential equations. By G. B. GUSTAFSON.....	187
Applications of Laplace transforms and their inverses. By CHARLES FOX.....	193
The analytic properties of $G_{2n}$ spaces. By DONALD O. KOEHLER.....	201
The radius of close-to-convexity of functions of bounded boundary rotation. By H. B. COONCE and M. R. ZIEGLER.....	207
Functions with real part greater than $\alpha$ . By CARL P. MCCARTY.....	211
On the location of zeros of second-order differential equations. By VADIM KOMKOV.....	217

#### C. APPLIED MATHEMATICS

Continuum embedded eigenvalues in a spatially cutoff $P(\phi)_2$ field theory. By BARRY SIMON.....	223
Error bounds for Galerkin's method for monotone operator equations. By MARTIN H. SCHULTZ.....	227

#### D. GEOMETRY

Closed convex hypersurfaces with second fundamental form of constant curvature. By ROLF SCHNEIDER.....	230
On an integral formula for closed hypersurfaces of the sphere. By CHORNG-SHI HOUH.....	234
On convex subsets of a polytope. By W. R. HARE, JR. and C. R. SMITH.....	238
On closed curves in Minkowski spaces. By H. S. WITSENHAUSEN.....	240

#### E. LOGIC AND FOUNDATIONS

Ordinal sum-sets. By MARTIN M. ZUCKERMAN.....	242
Weak partition relations. By ANDREAS BLASS.....	249

#### G. TOPOLOGY

Contractible Hilbert cube manifolds. By T. A. CHAPMAN.....	254
Map bordism of maps. By R. E. STONG.....	259
The Whitney technique for Poincaré complex embeddings. By J. P. E. HODGSON.....	263
Metritization of symmetric spaces and regular maps. By HAROLD W. MARTIN.....	269
Compact spaces and products of finite spaces. By DOUGLAS HARRIS.....	275
Another locally connected Hausdorff continuum not connected by ordered continua. By J. L. CORNETTE and B. LEHMAN.....	281
The topological complementation theorem à la Zorn. By PAUL S. SCHNARE.....	285
Simply-connected branched coverings of $S^3$ . By C. McA. GORDON and W. HEIL.....	287
A countable connected Urysohn space containing a dispersion point. By V. KANNAN.....	289
Euclidean neighborhoods in compact semigroups. By JOHN D. MCCHAREN.....	291

#### SHORTER NOTES

On a theorem of Rudin. By DONALD R. CHALICE.....	296
On semibounded differential operators. By HARRY HOCHSTADT.....	298
A factorable weight with zero Szegő infimum. By BERRIEN MOORE III.....	301
A note on some characterizations of Sidon sets. By RON C. BLEI.....	303
A note on the compact elements of $C^*$ -algebras. By KARI YLINEN.....	305
Nonnegative matrices with nonnegative inverses. By RALPH DEMARR.....	307



# CONTENTS\*

Vol. 35, No. 2

OCTOBER 1972

Whole No. 160

	Page
A. ALGEBRA AND NUMBER THEORY	
Quadratic Jordan algebras whose elements are all invertible or nilpotent. By KEVIN McCRIMMON .....	309
A splitting ring of global dimension two. By JOHN D. FUELBERTH and MARK L. TEPLY .....	317
On the order of some error functions related to $k$ -free integers. By V. S. JOSHI ..	325
Nodal algebras defined by skew-symmetric bilinear forms. By JERRY GOLDMAN ..	333
A note on Janko's simple group of order 175,560. By E. SHULT .....	342
A characterization of exchange rings. By G. S. MONK .....	349
On subfields of countable codimension. By A. BIAŁYŃICKI-BIRULA .....	354
Injective dimension and completeness. By M. BORATYŃSKI .....	357
Henselian fields and solid $k$ -varieties. II. By GUSTAVE EFROYMSON .....	362
A note on higher derivations and integral dependence. By WILLIAM C. BROWN ..	367
Gauss' lemma. By HWA TSANG TANG .....	372
Locally affine ring extensions of a noetherian domain. By WILLIAM HEINZER ...	377
The local rings of global dimension two. By WOLMER V. VASCONCELOS .....	381
The Schur index and roots of unity. By G. J. JANUSZ .....	387
On the equivalence of three local theorem techniques. By K. K. HICKIN and J. M. PLOTKIN .....	389
Orders in self-injective cogenerator rings. By ROBERT C. SHOCK .....	393
On the automorphism group of a finite modular $p$ -group. By RICHARD M. DAVITT and ALBERT D. OTTO .....	399
On the isomorphisms between certain congruence groups. By ROBERT E. SOLAZZI ..	405
Rational functions representing all residues mod $p$ . II. By L. J. MORDELL .....	411
Normal subgroups contained in the Frattini subgroup. By W. MACK HILL and CHARLES R. B. WRIGHT .....	413
B. ANALYSIS	
On the consistency theorem in matrix summability. By ROBERT E. ATALLA .....	416
Uniqueness and norm convexity in the Cauchy problem for evolution equations with convolution operators. By MONTY J. STRAUSS .....	423
Generalizations of results of Agmon and Nirenberg to the Cauchy problem for evolution equations. By MONTY J. STRAUSS .....	431
On the characterization of Abelian $W^*$ -algebras. By J. W. JENKINS .....	436
The Kobayashi distance induces the standard topology. By THEODORE J. BARTH ..	439
The convergence almost everywhere of Legendre series. By HARRY POLLARD ...	442
A global existence theorem for a nonautonomous differential equation in a Banach space. By DAVID LOWELL LOVELADY and ROBERT H. MARTIN, JR. ....	445
On linear Volterra integral equations of convolution type. By JOHN S. LEW .....	450
Asymptotic behavior of solutions of perturbed linear systems. By L. E. BOBISUD ..	457
A note on Kaplun limits and double asymptotics. By D. D. FREUND .....	464
Some unbounded functions of regular growth. By H. ARTHUR DEKLEINE and VLADIMIR DROBOT .....	471
A note on systems of linear integrodifferential equations. By ROBERT L. WHEELER ..	477
Commutants that do not dilate. By DOUGLAS N. CLARK .....	483

---

\* The volume index will contain a mapping showing the correspondence between sections A-G and the AMS (MOS) subject classification numbers.

Gauge functions and limit sets for nonautonomous ordinary differential equations. By H. K. WILSON .....	487
On the first boundary value problem for $[h(x, x', t)]' = f(x, x', t)$ . By WAYNE T. FORD .....	491
On $W^*$ embedding of $AW^*$ -algebras. By DIANE LAISON .....	499
Quasi-invariant Radon measures on groups. By CHANDRA GOWRISANKARAN ...	503
Separability in the strict and substrict topologies. By W. H. SUMMERS .....	507
Spectra of conservative matrices. By N. K. SHARMA .....	515
Norm reduction of averaging operators. By H. B. COHEN, M. A. LABBE and J. WOLFE .....	519

#### C. APPLIED MATHEMATICS

Generalized overrelaxation and Gauss-Seidel convergence on Hilbert space. By MICHAEL P. HANNA .....	524
Topological properties of the efficient point set. By BEZALEL PELEG .....	531

#### D. GEOMETRY

Surfaces with maximal Lipschitz-Killing curvature in the direction of mean curva- ture vector. By CHORNG-SHI HOUH .....	537
Integrably parallelizable manifolds. By VAGN LUNDGAARD HANSEN .....	543
Sums of distances between points on a sphere. By KENNETH B. STOLARSKY .....	547
Tangent bundles of homogeneous spaces are homogeneous spaces. By R. W. BROCKETT and H. J. SUSSMANN .....	550

#### E. LOGIC AND FOUNDATIONS

On the number of solutions of Diophantine equations. By MARTIN DAVIS .....	552
--	-----

#### F. STATISTICS AND PROBABILITY

Subfair red-and-black with a limit. By DAVID C. HEATH, WILLIAM E. PRUITT and WILLIAM D. SUDDERTH .....	555
Further comments on the continuity of distribution functions obtained by super- position. By BARTHEL W. HUFF .....	561

#### G. TOPOLOGY

Some properties of special functions derived from the theory of continuous trans- formation groups. By MRINAL KANTI DAS .....	565
Filter characterizations of $C$ - and $C^*$ -embeddings. By JOHN WILLIAM GREEN ...	574
On embedding annuli in $M^3$ . By C. D. FEUSTEL .....	581
A cobordism. By R. E. STONG .....	584
$\lambda$ -equivariant bordism of maps. By ROBERT L. RINNE .....	587
Immersions and embeddings of projective spaces. By S. FEDER and D. M. SEGAL	590
Topologically complete groups. By LAWRENCE G. BROWN .....	593
Closed ideals in $C(X)$ . By PHILIP NANZETTA and DONALD PLANK .....	601
Toroidal arcs are cellular. By TOM KNOBLAUCH .....	607
Smooth structure and signature of codimension 2 embeddings. By DIETER ERLE	611
Knots without unknotted incompressible spanning surfaces. By HERBERT C. LYON	617
Corrections to "The structure of $B[c]$ and extensions of the concept of conull matrix" By H. I. BROWN, D. R. KERR and H. H. STRATTON .....	621