## PROCEEDINGS

OF THE

## American Mathematical Society

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George B. Seligman, Department of Mathematics, Yale University, New Haven, Connecticut 06520

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[^1]:    * The volume index will contain a mapping showing the correspondence between sections A-G and the AMS (MOS) subject classification numbers.

