

# St. Petersburg Mathematical Journal

(Formerly Leningrad Mathematical Journal)

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Volume 17 Number 1 2006

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*A Translation of*

РОССИЙСКАЯ АКАДЕМИЯ НАУК

АЛГЕБРА

И

АНАЛИЗ

ТОМ 17 ВЫПУСК 1 2005



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American Mathematical Society

Providence, Rhode Island USA

ISSN 1061-0022

# ST. PETERSBURG MATHEMATICAL JOURNAL

(Formerly Leningrad Mathematical Journal)

*A translation of the Russian bimonthly*

Алгебра и анализ

“Наука”, С.-Петербургское отделение, 2005 г.

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**St. Petersburg Mathematical Journal** is published bimonthly by the American Mathematical Society, 201 Charles Street, Providence, RI 02904-2294 USA. Periodicals postage paid at Providence, Rhode Island. Postmaster: Send address changes to St. Petersburg Mathematical Journal, American Mathematical Society, 201 Charles Street, Providence, RI 02904-2294 USA.

**Manuscripts** should be addressed to “Algebra i Analiz”, St. Petersburg Publishing Company of the Russian Academy of Sciences, Mendeleevskaya Liniya 1, St. Petersburg 199034, Russia. Submitting simultaneously a tex-file to the address [pmj@pdmi.ras.ru](mailto:pmj@pdmi.ras.ru) is highly appreciated.

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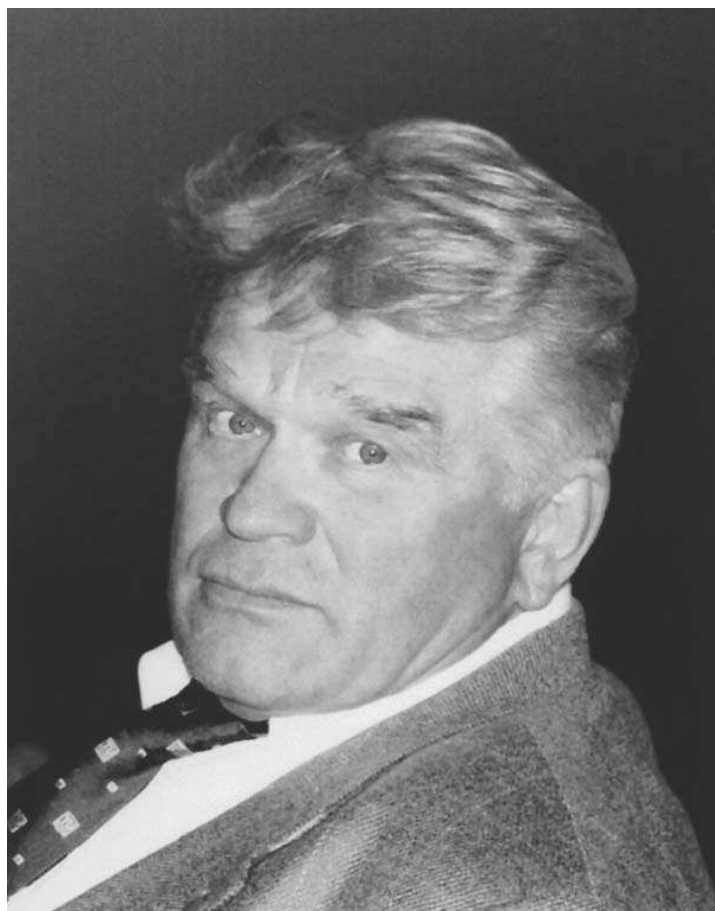
This journal is indexed in *Mathematical Reviews* and *Zentralblatt MATH*.

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10 9 8 7 6 5 4 3 2 1      11 10 09 08 07 06



**The Editorial Board  
cordially congratulates  
Ludwig Dmitrievich FADDEEV  
on his birthday**

(Continued from back cover)

<i>Bobenko A. I., Matthes D., Suris Yu. B.</i> Nonlinear hyperbolic equations in surface theory: integrable discretizations and approximation results . . . . .	53
<i>Боголюбов Н. М., Мальшиев К.</i> Функциональное интегрирование и двухточечная корреляционная функция одномерного бозе-газа в гармоническом потенциале . . . . .	84
<i>Boos H., Jimbo M., Miwa M., Smirnov F., Takeyama Y.</i> A recursion formula for the correlation functions of an inhomogeneous XXX model. . . . .	115
<i>Гуревич Д. И., Пятов П. Н., Сапонов П. А.</i> Теорема Кэли-Гамильтона для квантовых матричных алгебр $GL(m n)$ типа . . . . .	160
<i>Jackiw R.</i> A kink in a funny place . . . . .	183
<i>Hikami K., Kirillov A. N.</i> Hypergeometric generating function of $L$ -function, Slater's identities, and quantum invariant. . . . .	190
<i>Кашаев Р. М.</i> О самосопряженных расширениях одного разностного оператора. . . . .	209
<i>Kitaev A. V.</i> Grothendieck's dessins d'enfants, their deformations and algebraic solutions of the sixth Painlevé and Gauss hypergeometric equations. . . . .	224
<i>Скриганов М. М., Соболев А. В.</i> Асимптотические оценки для спектральных зон периодических операторов Шрёдингера . . . . .	276



**St. Petersburg Mathematical Journal**  
(Formerly Leningrad Mathematical Journal)

Volume 17    Number 1    2006    (First of 6 Numbers)

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**Research Papers**

<b>E. Balslev and A. Venkov</b> , On the relative distribution of eigenvalues of exceptional Hecke operators and automorphic Laplacians .....	1
<b>A. I. Bobenko, D. Matthes, and Yu. B. Suris</b> , Nonlinear hyperbolic equations in surface theory: Integrable discretizations and approximation results .....	39
<b>N. M. Bogoliubov and C. Malyshev</b> , Functional integration and the two-point correlation function of the one-dimensional Bose gas in a harmonic potential .....	63
<b>H. Boos, M. Jimbo, T. Miwa, F. Smirnov, and Y. Takeyama</b> , A recursion formula for the correlation functions of an inhomogeneous XXX model .....	85
<b>D. I. Gurevich, P. N. Pyatov, and P. A. Saponov</b> , Cayley–Hamilton theorem for quantum matrix algebras of $GL(m n)$ type .....	119
<b>R. Jackiw</b> , A kink in a funny place .....	137
<b>K. Hikami and A. N. Kirillov</b> , Hypergeometric generating function of $L$ -function, Slater's identities, and quantum invariant .....	143
<b>R. M. Kashaev</b> , On selfadjoint extensions of some difference operator ...	157
<b>A. V. Kitaev</b> , Grothendieck's dessins d'enfants, their deformations, and algebraic solutions of the sixth Painlevé and Gauss hypergeometric equations .....	169
<b>M. M. Skriganov and A. V. Sobolev</b> , Asymptotic bounds for spectral bands of periodic Schrödinger operators .....	207

**СОДЕРЖАНИЕ**

**Статьи**

<i>Balslev E., Venkov A.</i> On the relative distribution of eigenvalues of exceptional Hecke operators and automorphic Laplacians .....	5
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(Continued on inside back cover)



1061-0022(2006)17:1;1-1