St. Petersburg Mathematical Journal

(Formerly Leningrad Mathematical Journal)

Volume 19 Number 1 2008

A Translation of

РОССИЙСКАЯ АКАДЕМИЯ НАУК

АЛГЕБРА И АНАЛИЗ

ТОМ 19 № 1 2007

American Mathematical Society

Providence, Rhode Island USA
ISSN 1061-0022

ST. PETERSBURG MATHEMATICAL JOURNAL
(Formerly Leningrad Mathematical Journal)
A translation of the Russian bimonthly
Алгебра и анализ
"Наука", С.-Петербургское отделение, 2007 г.

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December 25, 2005, was the 85th birthday of the widely known Russian mathematician and remarkable man, Professor Viktor Abramovich Zalgaller.
His collaborators in the Mathematical Institute and St. Petersburg University, his colleagues and friends, cordially congratulate him and wish him good health and happiness.

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St. Petersburg Mathematical Journal VOLUME 19 NUMBER 1 2008