

# St. Petersburg Mathematical Journal

(Formerly Leningrad Mathematical Journal)

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Volume 21 Number 5 October 2010

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*A Translation of*

РОССИЙСКАЯ АКАДЕМИЯ НАУК

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Алгебра и анализ

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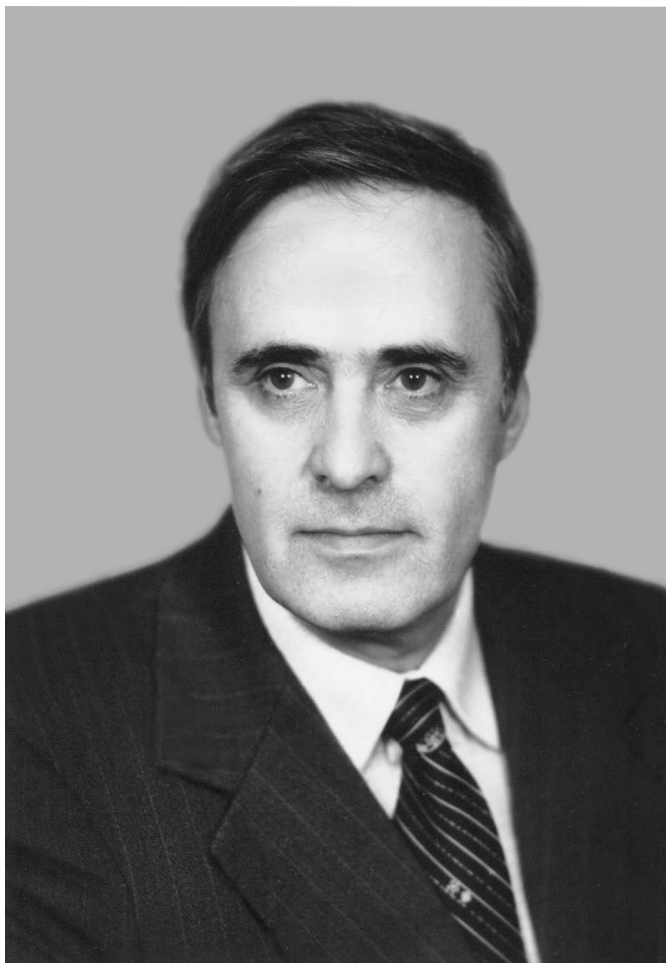
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**Mikhail Shlemovich Birman**  
January 17, 1928–July 2, 2009

Professor Birman was an editor of our journal since its inception.  
With great sorrow, we announce his death.

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