

# St. Petersburg Mathematical Journal

(Formerly Leningrad Mathematical Journal)

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Volume 26 Number 5 October 2015

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*A Translation of*

РОССИЙСКАЯ АКАДЕМИЯ НАУК

АЛГЕБРА  
И  
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# ST. PETERSBURG MATHEMATICAL JOURNAL

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Алгебра и анализ

“Наука”, С.-Петербургское отделение, 2014 г.

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