

# St. Petersburg Mathematical Journal

(Formerly Leningrad Mathematical Journal)

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Volume 29 Number 4 August 2018

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*A Translation of*

РОССИЙСКАЯ АКАДЕМИЯ НАУК

АЛГЕБРА  
И  
АНАЛИЗ

ТОМ 29 № 4 2017



AMERICAN  
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Providence, Rhode Island USA

# ST. PETERSBURG MATHEMATICAL JOURNAL

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*A translation of the Russian bimonthly*

Алгебра и анализ

“Наука”, С.-Петербургское отделение, 2017 г.

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