

# Theory of Probability and Mathematical Statistics

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Number 92 2016

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*A Translation of*

ТЕОРІЯ  
ЙМОВІРНОСТЕЙ ТА  
МАТЕМАТИЧНА  
СТАТИСТИКА

ВИПУСК 92 2015



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# **THEORY OF PROBABILITY AND MATHEMATICAL STATISTICS**

*A translation of*

## **ТЕОРІЯ ЙМОВІРНОСТЕЙ ТА МАТЕМАТИЧНА СТАТИСТИКА**

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