

# Theory of Probability and Mathematical Statistics

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Number 96 2018

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*A Translation of*

ТЕОРІЯ  
ЙМОВІРНОСТЕЙ ТА  
МАТЕМАТИЧНА  
СТАТИСТИКА

ВИПУСК 96 2017



AMERICAN  
MATHEMATICAL  
SOCIETY

Providence, Rhode Island USA

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ТЕОРІЯ ЙМОВІРНОСТЕЙ ТА МАТЕМАТИЧНА СТАТИСТИКА

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