Meeting: 1000, Albuquerque, New Mexico, SS 5A, Special Session on Categories and Operads in Topology, Geometry, Physics and Other Applications

1000-57-48Jozef H Przytycki* (przytyck@gwu.edu), Department of Mathematics, George Washington
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Sikora. Categorification of the Kauffman bracket skein module of $F \times I$.

We define Khovanov homology, $H_{i,j,k}$ for links in products of surfaces and an interval and in twisted *I*-bundles over unorientable surfaces (excluding RP^2). We show how to stratify this homology so that (in the product case, $F \times I$) it categorifies the Kauffman bracket skein module (KBSM) of $F \times I$. That is, for any link *L* in $F \times I$ we can recover coefficients of L in the standard basis B(F) of the KBSM of $F \times I$. In other words if $L = \sum_b a_b(A)b$ where the sum is taken over all basic elements, $b \in B(F)$, then each coefficient $a_b(A)$ can be recovered from polynomial Euler characteristics of the stratified Khovanov homology. In the case of unorientable F we are able to recover coefficients $a_b(A)$ only partially. We propose another basis of the KBSM for which categorification seems to be possible even for unorientable F (we use cores of Möbius bands several times even if they intersect one another). (Received August 06, 2004)