Meeting: 1007, Santa Barbara, California, SS 13A, Special Session on Arithmetic Geometry

1007-11-28 B.D. (Byoung-du) Kim\* (byoung@math.stanford.edu), Department of Mathematics, Stanford University, Stanford, CA 94305. The Parity Conjecture of Elliptic Curves and Algebraic Functional Equations at Primes with Supersingular Reduction.

In number theory and arithmetic geometry, we expect an algebraic object such as a Mordell-Weil group of an abelian variety and an analytic object such as an *L*-function of an abelian variety are inherently related. A classic example of this belief is the Birch and Swinnerton-Dyer (BSD) conjecture. The BSD conjecture predicts that the rank of a Mordell-Weil group of an elliptic curve is equal to the order of zero at s = 1 of an *L*-function of the same elliptic curve. Its modulo 2 version, the parity conjecture, is a good evidence of the BSD conjecture if proved. In this paper, we prove the parity conjecture when p is a good supersingular reduction prime. Using a similar idea, we also prove the algebraic functional equations for  $\pm$ -Selmer groups defined by S. Kobayashi. (Received December 12, 2004)