1007-16-206 Pavel Etingof and Alexei Oblomkov* (oblomkov@math.mit.edu), 2-092, 77 Massachusetts Ave., Cambridge, MA 02139, and Eric Rains. Generalized double affine Hecke algebras of rank 1 and quantized Del Pezzo surfaces.

To star-shaped simply laced affine Dynkin diagram D one can use a standard procedure to attach a crystallographic group G. We define a flat deformation H(t,q) of the group algebra $\mathbb{C}[G]$. If $D = D_4$, then H(t,q) is the double affine Hecke algebra of rank 1. We prove that H(t,q) is the universal deformation of the twisted group algebra of G, and that this deformation is compatible with certain filtrations on C[G]. If q is a root of unity, then for generic t the algebra H(t,q) is an Azumaya algebra, and its center is the function algebra on an affine del Pezzo surface. For generic q, the spherical subalgebra eH(t,q)e provides a quantization of such surfaces. Talk is based on the joint paper with P. Etingof and E.Rains. (Received February 21, 2005)