Meeting: 1007, Santa Barbara, California, AMS CP 1, Session for Contributed Papers

1007-20-87 Richard P. Kubelka* (kubelka@math.sjsu.edu), Department of Mathematics, San Jose State University, San Jose, CA 95192-0103. The 2-Dog Group. Preliminary report.
The speaker will discuss the solution of a problem suggested by his two dachshunds, Fritz and Sasha. To wit, in what ways can two dogs entangle themselves and their walker during a stroll around the block? And, furthermore, how much of that entanglement can be resolved by countermoves on the part of the walker?

The answer involves $\mathcal{D}_{2}$, the 2-Dog Group, an infinite, nonabelian, torsion-free group-reminiscent of Artin's Braid Groups-and an index-two subgroup $\mathcal{W}$, the walker subgroup. The speaker will give a complete description of these groups in terms of generators and relations; give a minimal presentation of $\mathcal{D}_{2}$-with two generators and one relation; and show that these groups can actually be interpreted as subgroups of the classical Braid Group $B_{3}$. In the process he will show by group-theoretic means that, as far as dog walks are concerned, the right hand doesn't know what the left hand is doing. (Received February 03, 2005)

