In 1988 Brion gave a formula for the integer points in a rational polytope in $\mathbb{R}^{d}$ in terms of certain rational generating functions associated to its vertices. His proof used the equivariant $K$-theory of singular toric varieties, and his formula led to Barvinok's polynomial-time algorithm for the integer points in a polytope.

I will present a proof of Brion's Theorem based on simple counting, using the technique of irrational decompositions. This is joint work with Beck and Haase. I will also describe how Koeppe uses irrational decompositions to dramatically improve the performance of Barvinok's algorithm. (Received September 07, 2006)

