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Plamen Stefanov* (stefanov@math.purdue.edu), Department of Mathematics, Purdue University, West Lafayette, IN 47907, and Gunther Uhlmann. Tensor tomography and lens rigidity on a class of non-simple Riemannian manifolds with boundary.

We study a class of compact manifolds M with boundary equipped with a Riemannian metric g, not necessarily convex, with possible conjugate points. We study the geodesic ray transform of integrals of symmetric 2-tensor fields over geodesics connecting boundary points. Moreover, we restrict the set of geodesics over which we know the integrals to an open one such that its conormal bundle covers T^*M . Under some conditions on the pairs of the conjugate points and on the topology of M, we show that for an open dense set of g's, the geodesic ray transform recovers uniquely the tensor up to a potential field, and moreover, there is a stability estimate uniform under small perturbations of g. That set includes all real analytic metrics satisfying the assumptions. The methods rely on analytic and classical microlocal analysis. We discuss applications of this result to the non-linear lens rigidity problem of recovering g from the scattering relation on the boundary. (Received August 28, 2006)