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Yasuyuki Kachi* (kachi@math.ku.edu), Snow Hall, 1460 Jayhawk Boulevard, Lawrence, KS 66045-7523. *Birational Equivalence, Linear Systems, and Desingularization.*

I introduce an object $\text{Spv } X$ which represents the birational equivalence class of an algebraic variety X and which admits a morphism to X . $\text{Spv } X$ is a functor that mimics the usual $\text{Hom}(\text{Spec } (*), X) : (\text{Ring}) \longrightarrow (\text{Set})$. Namely, I define $\text{Spv } X$ as $\text{Hom}(\text{Spec } HVR_n(*), X)$, using some universal coefficient ring $HVR_n(*)$. I also define the completion $\text{Spv } ^\wedge X$, using linear systems, which turns out to coincide with the categorical limit of proper varieties birational to X . In the course it arises a group functor SG_n which is a uniform analog of GL_n and which reflects a composition algorithm of blow-ups. I show that Cutkosky's factorization of birational correspondence is interpreted precisely as the transitivity of the action of $SG_n(k)$ on "the classifying space" $\mathcal{S}_n(k)$ consisting of regular local subrings of $HVR_n(k)$. I show that Kronecker's principle, that (roughly speaking) dictates how the regular local subrings are immersed in $HVR_n(k)$, reproduces the feasibility of local desingularization, in an arbitrary characteristic, with a note that Kronecker's principle fails for "the complete analog" of $HVR_n(k)$ in $k((t_n))(\dots)((t_1))$. (Received August 29, 2006)