1020-47-159 Gary Weiss and Vrej Zarikian* (zarikian@usna.edu), 572C Holloway Road, Annapolis, MD 21402. 3-Paving Small Matrices and the Kadison-Singer Extension Problem. Preliminary report. The Kadison-Singer Problem, posed in 1959, asks whether every pure state on the diagonal of $B(\ell^2)$ extends uniquely to a pure state on all of $B(\ell^2)$. It is equivalent to a variety of important problems (cf. Casazza and Tremain, The Kadison-Singer Problem in Mathematics and Engineering, Proc. Natl. Acad. Sci. USA 103 (2006)). Among these reformulations is Anderson's Paving Conjecture from 1979:

> Given $0 < \varepsilon < 1$, there exists a $k \in \mathbb{N}$ such that for any $n \in \mathbb{N}$ and any $A \in M_n(\mathbb{C})$ with zero diagonal, there exist diagonal projections $P_1, P_2, ..., P_k \in M_n(\mathbb{C})$ such that $P_1 + P_2 + ... + P_k = I$ and

> > $||P_j A P_j|| \le \varepsilon ||A||, \ 1 \le j \le k.$

In spite of significant progress by Berman-Halpern-Kaftal-Weiss (1988) and Bourgain-Tzafriri (1991), the Paving Conjecture (and therefore the Kadison-Singer Problem) remain open. In this talk, we examine the Paving Conjecture for "small" parameter values: k = 3 and $n \le 10$. Using a combination of graph theory and operator theory, we determine the sharp ε for n = 4, 5, 6. Using different methods, we produce examples of "bad pavers" of size n = 7, 10. (Received August 26, 2006)