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Charles Chidume* (chidume@ictp.it), International Centre for Theoretical Physics, Trieste, Italy. *Convergence of Iterates to a Common Fixed Point of a Family of Mappings.*

Let E be a real reflexive Banach space with uniformly Gâteaux differentiable norm. Let K be a nonempty closed convex subset of E . Suppose that every nonempty closed convex bounded subset of E has the fixed point property for nonexpansive mappings. Let T_1, T_2, \dots, T_N be a family of nonexpansive self mappings of K , with $F := \bigcap_{i=1}^N \text{Fix}(T_i) = \text{Fix}(T_N T_{N-1} \dots T_1) = \text{Fix}(T_1 T_N \dots T_2) = \dots = \text{Fix}(T_{N-1} T_{N-2} \dots T_1 T_N) \neq \emptyset$. Let $\{\lambda_n\}$ be a sequence in $(0, 1)$ satisfying the following conditions: $C1 : \lim \lambda_n = 0$; $C2 : \sum \lambda_n = \infty$. For a fixed $\delta \in (0, 1)$, define $S_n : K \rightarrow K$ by $S_n x := (1 - \delta)x + \delta T_n x$, $\forall x \in K$ where $T_n = T_{n \bmod N}$. For arbitrary fixed $u, x_0 \in K$, let $B := \{x \in K : S_N S_{N-1} \dots S_1 x = \gamma x + (1 - \gamma)u, \text{ for some } \gamma > 1\}$ be bounded and the sequence $\{x_n\}$ be defined iteratively by

$$x_{n+1} = \lambda_{n+1}u + (1 - \lambda_{n+1})S_{n+1}x_n, \text{ for } n \geq 0.$$

Assume $\lim_{n \rightarrow \infty} \|T_n x_n - T_{n+1} x_n\| = 0$. Then, $\{x_n\}$ converges strongly to a common fixed point of the family T_1, T_2, \dots, T_N . (Received August 28, 2006)