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Lee R Gibson* (lrgibs01@gmail.com), Department of Mathematics, 328 Natural Sciences Building, University of Louisville, Louisville, KY 40292. *The Mass of Sites Visited by a Random Walk on an Infinite Graph*. Preliminary report.

In 1979 Donsker and Varadhan proved that for an explicitly computed constant $c(d, \nu)$ the simple random walk in \mathbb{Z}^d satisfies

$$\lim_{n \rightarrow \infty} n^{-d} \log \mathbb{E} [\exp \{-\nu R_{n^{d+2}}\}] = -c(d, \nu),$$

where R_n denotes the stationary measure of the sites visited by the random walk. Here we use a simple coarse graining technique to show that when $V(x, n)$ (the stationary measure of path length balls about x) does not depend asymptotically on x

$$\log \mathbb{E}^x [\exp \{-\nu R_{n^\beta V(x, n)}\}] \simeq -V(x, n),$$

either when $V(x, n)$ satisfies volume doubling and the random walk generator satisfies a Poincaré inequality with parameter $\beta = 2$ or when the random walk transition probabilities satisfy a two-sided sub-Gaussian estimate with parameter $\beta > 2$. These results apply, for example, to the Cayley graphs of finitely generated groups with polynomial volume growth and to certain fractal-like graphs. (Received July 05, 2006)