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Noah Prince* (nprince@math.uiuc.edu). *Nordhaus-Gaddum Bounds for k -Domination in Graphs.*

A k -dominating set of a graph G is a set S of vertices of G such that every vertex not in S has at least k neighbors in S . The k -domination number of G , written $\gamma_k(G)$, is the size of the smallest k -dominating set in G . We derive sharp upper and lower bounds on $\gamma_k(G) + \gamma_k(\overline{G})$ and $\gamma_k(G)\gamma_k(\overline{G})$, where \overline{G} is the complement of G . We use the results for $k = 2$ to prove a conjecture of Alon, Balogh, Bollobás, and Szabó on game domination numbers. (Received February 08, 2008)