Tao Jiang* (jiangt@muohio.edu), Department of Mathematics and Statistics, Miami University, Oxford, OH. Properly colored cycles in edge-colored graphs. Preliminary report.
We are interested in color patterns forced in edge-colorings of a host graph satisfying certain constrants. Such problems are inspired by the Canonical Ramsey Theorem. In this talk we focus on cycles, which as in the Turan problem form a degenerate case which is key to our understanding. We sketch a proof of a conjecture by Aexnovich, the speaker, and Tuza that for each $k$ there is a constant $\lambda_{k}$ depending only on $k$ such that for large enough $n$ in every edge-coloring of $K_{n}$ in which at least $\lambda_{k}$ different colors are used at each vertex one can always find a properly colored cycle of length exactly $k$. The value of $\lambda_{k}$ given in the proof is large. It remains an interesting problem to find better bounds on $\lambda_{k}$. (Received February 13, 2008)

