1038-05-213 Jozsef Balogh (jobal@math.uiuc.edu), Wojciech Samotij (samotij2@uiuc.edu) and Sujith Vijay* (sujith@math.uiuc.edu), Department of Mathematics, University of Illinois at Urbana-Champaign, 1409 W Green St, Urbana, IL 61801. The Minimal Size of Restricted Difference Bases.

A graph labelling problem of considerable interest in additive combinatorics is the minimal size of restricted difference bases of $\{0, 1, ..., n\}$. The objective is to find the least order k = k(n) of a complete graph which admits a labelling of vertices with integers in $\{0, 1, ..., n\}$ such that every integer from 1 to n is induced on some edge as the difference between the labels on its endpoints.

Rédei and Rényi showed in 1949 that $k(n)/\sqrt{n}$ approaches a limit for large n and established a non-trivial lower bound of $\sqrt{2 + \frac{4}{3\pi}}$ on the limiting ratio. The best lower and upper bounds currently known are due to Leech and Wichmann, respectively. We obtain a slight improvement on the lower bound by refining the ideas in the original paper of Rédei and Rényi. (Received February 10, 2008)