Michael Ferrara* (mjf@uakron.edu), The University of Akron, and John Schmitt, Middlebury College. A Lower Bound for Potentially H-graphic Sequences.
We consider a variation of the classical Turán-type extremal problem. Let $\pi$ be an $n$-element graphic sequence, and $\sigma(\pi)$ be the sum of the terms in $\pi$. Let $H$ be a graph. We wish to determine the smallest $m$ such that any $n$-term graphic sequence $\pi$ having $\sigma(\pi) \geq m$ has some realization containing $H$ as a subgraph. Denote this value $m$ by $\sigma(H, n)$. For an arbitrarily chosen $H$, we construct a graphic sequence $\pi^{*}(H, n)$ such that $\sigma\left(\pi^{*}(H, n)\right)+2 \leq \sigma(H, n)$. Furthermore, we conjecture that equality holds in general, as this is the case for all choices of $H$ where $\sigma(H, n)$ is currently known. We support this conjecture by examining the complements of triangle-free graphs and showing that the conjecture holds in this broad class. (Received January 23, 2008)

