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Gábor Fejes Tóth* (gfejes@renyi.hu), Rényi Institute, POBox 127, Budapest, 1364, Hungary. *The moment theorem for convex sets.*

We prove the following

Theorem. *Let R be a convex domain and P a set of $n \geq 2$ points in the plane. Let H be a regular hexagon centered at the origin with $\text{area}(H) = \text{area}(R)/n$. Then we have for any non-increasing function f defined for non-negative reals*

$$\int_R f(\min_{p \in P} \|p - x\|) dx \leq n \int_H f\|x\| dx.$$

For a non-decreasing function f the inequality stands with the reversed sign.

This is a generalization of the “moment theorem” which was proved previously for the case when R is a convex polygon with at most six sides. (Received February 26, 2007)