

1026-52-93

Ralph Howard* (howard@math.sc.edu), Department of Mathematics, University of South Carolina, Columbia, SC 29208, **Dmitry Ryabogin** (ryabs@math.ksu.edu), Mathematics Department, 138 Cardwell Hall, Kansas State University, Manhattan, KS 66506-2602, **Anamaria Rusu** (rusu@math.sc.edu), Department of Mathematics, University of South Carolina, Columbia, SC 29208, and **Artem Zvavitch** (zvavitch@math.kent.edu), Department of Mathematical Sciences, Mathematics and Computer Science Building, Summit Street, Kent, OH 44242.

Determining Symmetric Convex Bodies by the Perimeters of Their Central Sections.

Let \mathcal{P}_k^n be the collection of all C^1 convex bodies K in \mathbf{R}^n symmetric about the origin with the property that for all k -dimensional linear subspaces P of \mathbf{R}^n $V_{k-1}(P \cap \partial K) = V_{k-1}(P \cap \partial \mathbf{B}^n)$ where \mathbf{B}^n is the Euclidean ball. (That is $K \in \mathcal{P}_k^n$ is a centrally convex body with C^1 boundary and the property that the $(k-1)$ -dimensional “parameter” of $P \cap K$ is the same as that of $P \cap \mathbf{B}^n$ for all k -dimensional central sections of K .) We show that in this class the ball is isolated in the sense that all one parameter analytic deformations of the ball in \mathcal{P}_k^n are constant. This gives evidence to support the conjecture that if K_1 and K_2 are two convex bodies symmetric about the origin whose sections by any k -dimensional plane through the origin have equal perimeters, then $K_1 = K_2$, a question posed by Richard Gardner in his book *Geometric Tomography* in the case $k = 2$ and $n = 3$. (Received February 16, 2007)