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**Paul Pollack\*** (ppollac@illinois.edu), 1409 West Green Street, Department of Mathematics, MC-382, University of Illinois at Urbana-Champaign, Urbana, IL 61801. *Some problems concerning the fraction  $\sigma(n)/n$ .*

Let  $\sigma(n)$  denote the sum of the divisors of the natural number  $n$ . The ratio  $\sigma(n)/n$  has been of interest ever since the ancient Greeks, who classified numbers as *deficient*, *perfect*, or *abundant* according as  $\sigma(n)/n$  is less than, equal, or greater than 2 (respectively). We survey what is known about this ratio, paying particular attention to the contributions of Erdős. We also describe some new results of the speaker concerning the amount of cancellation when  $\sigma(n)/n$  is put in lowest terms. These results are connected with some 50-year old claims of Erdős. (Received February 03, 2009)