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Department of Maths & Stats, McLean Hall, 106 Wiggins Road, Saskatoon, SK S7N 5E6, Canada,
and **J. Cimpric** and **M. Marshall**. *Positivity in power series rings.*

Let $A = \mathbb{R}[x] := \mathbb{R}[x_1, \dots, x_n]$ be the ring of polynomials in n variables with real coefficients. A preordering of A is a subset which contains all f^2 for $f \in A$, and is closed under addition and multiplication. For a finite subset $S = \{g_1, \dots, g_s\}$ of A , we write $T = T_S$ for the preordering of A finitely generated by S , and $K = K_S$ for the set of all $x \in \mathbb{R}^n$ satisfying $g_i(x) \geq 0$ for $i = 1, \dots, s$ (the basic closed semialgebraic set defined by S). We write $\text{Psd}(K)$ for the set of all polynomials that are nonnegative on K . The preordering T is said to be saturated if $T = \text{Psd}(K)$. Finitely generated saturated preorderings are particularly interesting since in this case, every nonnegative polynomial on the semialgebraic set has a concrete representation using sums of squares and the defining polynomials $\{g_1, \dots, g_s\}$. In this talk we investigate what geometric properties of S imply that T is saturated. We know that T is never saturated if $\dim(K) \geq 3$. The case $\dim(K) \leq 1$ is well understood. We focus here on the 2- dimensional compact case. (Received February 01, 2009)