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Alexander Yu. Solynin* (alex.solynin@ttu.edu), Texas Tech University, Department of Mathematics and Statistics, Lubbock, TX 79409. *A variant of Schwarz lemma for meromorphic functions and estimates for the hyperbolic metric.*

I will discuss a generalization of the Schwarz lemma for the class of meromorphic functions $f(z)$ mapping the unit disk \mathbb{D} onto Riemann surfaces \mathcal{R} with bounded in mean radial distances from $f(0)$ to the boundary of \mathcal{R} . Our variant of the Schwarz lemma implies a stronger form of the Landau-Toeplitz theorem, which extends the classical Schwarz lemma for the class of analytic functions $f(z)$ such that the diameter of $f(\mathbb{D})$ does not exceed 2. A new variant of the Schwarz lemma will be also given for the Carathéodory class of analytic functions having positive real part in \mathbb{D} . Our results lead to several improved estimates for the hyperbolic metric. (Received February 03, 2009)