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J. Cao (cao.7@nd.edu), Mathematics department, Notre Dame, IN 46556, and **Jian Ge*** (jge@nd.edu), Mathematics department, Notre Dame, IN 46556. *A new proof to Perelman's collapsing theorem for geometrization of 3-manifolds.* Preliminary report.

We will use an observation of Kasten Grove together with Perelman's convexity lemma to provide a simplified proof of Perelman's collapsing theorem of 3-manifold.

Theorem 1 (Perelman's Collapsing Theorem). Suppose that $\{(M_\alpha^3, g_{ij}^\alpha)\}_{\alpha \in \mathbb{Z}}$ is a sequence of compact oriented Riemannian manifolds, closed or with convex incompressible tori boundary, and $\omega^\alpha \rightarrow 0$. Assume that

1. for each point $x \in M_\alpha^3$ there exists a radius $\rho = \rho^\alpha(x)$, $0 < \rho < 1$, not exceeding the diameter of the manifold, such that the ball $B_{g^\alpha}(x, \rho)$ in the metric g_{ij}^α has volume at most $\omega^\alpha \rho^3$ and sectional curvatures of g_{ij}^α at least $-\rho^{-2}$;
2. each component of the boundary of M_α has diameter at most ω^α and has a topological trivial collar of length one, where the sectional curvatures are between $(-1/4 - \epsilon)$ and $(-1/4 + \epsilon)$

Then, for sufficiently large α , M_α^3 is diffeomorphic to a graph-manifold. (Received January 24, 2009)