The classical three gap theorem asserts that for a natural number $n$ and a real number $p$, there are at most three distinct distances between consecutive elements in the subset of $[0,1)$ consisting of the reductions modulo 1 of the first n multiples of p. I'll discuss analogues of this theorem pertaining to isometries of a Riemannian manifold $M$ and to equally spaced points along a geodesic in M. This talk is based on joint work with Ian Biringer. (Received July 27, 2009)

