1050-39-89Gabriel Lugo and Frank J Palladino* (fpalladino@math.sunysb.edu), 350 Circle Rd.,
Schomburg B103C, Stony Brook, NY 11794. Unboundedness for some classes of rational difference
equations. Preliminary report.

We study the rational difference equation

$$x_n = \frac{\alpha + x_{n-1}}{Cx_{n-2} + x_{n-3}}, n \in \mathbb{N}.$$

Particularly, we show that for non-negative α and C, whenever $C\alpha = 0$ and $C + \alpha > 0$, unbounded solutions exist for some choice of non-negative initial conditions. Moreover, we study the rational difference equation

$$x_n = \frac{\alpha + \beta x_{n-1} + x_{n-2}}{x_{n-3}}, n \in \mathbb{N}.$$

Particularly, we show that whenever $0 < \beta < \frac{1}{3}$ and $\alpha \in [0, 1]$, unbounded solutions exist for some choice of non-negative initial conditions. (Received February 27, 2009)