

1089-05-86

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Extremal graphs for Gallai's Conjecture on the minimum size of k -critical n -vertex

graphs. Preliminary report.

A graph G is k -critical if the chromatic number of G is k , but the chromatic number of every its proper subgraph is less than k . In particular, every graph with chromatic number k contains a k -critical subgraph. Dirac in 1957 posed the problem of finding the minimum number of edges, $f_k(n)$, in an n -vertex k -critical graph. It is well known that $f_3(n) = n$ for all odd $n \geq 3$, but for $k \geq 4$, the values of $f_k(n)$ were known only for small n . Gallai in 1963 conjectured that $f_k(n) = \frac{(k+1)(k-2)n-k(k-3)}{2(k-1)}$ for each $k \geq 4$ and $n \equiv 1 \pmod{k-1}$, $n \geq k$. Very recently, the authors proved this conjecture and determined the values of $f_4(n)$ for every $n \geq 6$. The aim of the talk is to prove a Brooks-type result: We describe all k -critical n -vertex graphs with exactly $\frac{(k+1)(k-2)n-k(k-3)}{2(k-1)}$ edges. As a corollary we determine the values of $f_5(n)$ for every $n \geq 7$. (Received February 03, 2013)