

1089-05-89

**Nantel Bergeron\***, York University, Dept. of Mathematics and Stat., Toronto, Ontario M3J1P3, Canada, and **C. Berg, F. Saliola, L. Serrano** and **M. Zabrocki**. *Immaculate basis and the non-commutative littlewood richardson rule.*

We have defined a new basis for  $NSym$ , the non-commutative symmetric functions. We called it the immaculate basis and denote it  $I_\alpha$  indexed by compositions  $\alpha$ . This basis has the property that the forgetful map  $\chi$  from  $NSym$  to symmetric function gives  $\chi(I_\alpha) = s_\alpha$  where  $s_\alpha = \det(h_{\alpha_i-i+j})$  is the Schur function defined by the Jacobi-Trudi determinant. In particular the  $s_\alpha$  make sense even for a composition  $\alpha$ .

we give versions of the right Pieri rule and non-commutative Littlewood-Richardson rules in this context. The non-commutative Littlewood-Richardson coefficient  $C_{\alpha,\lambda}^\beta$  are shown to be all positive (for a partition  $\lambda$ ) and satisfies a fascinating new relation.

We also construct indecomposable modules for the 0-Hecke algebra whose characteristics are the dual immaculate basis of the quasi-symmetric functions. (Received February 03, 2013)