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We approach the analysis of the extent of the projectivity of modules from a fresh perspective as we introduce the notion of relative subprojectivity. A module  $M$  is said to be  $N$ -subprojective if for every epimorphism  $g : B \rightarrow N$  and homomorphism  $f : M \rightarrow N$ , there exists a homomorphism  $h : M \rightarrow B$  such that  $gh = f$ . For a module  $M$ , the *subprojectivity domain of  $M$*  is defined to be the collection of all modules  $N$  such that  $M$  is  $N$ -subprojective. Modules whose subprojectivity domain is smallest as possible will be called *subprojectively poor* (*sp-poor*) or *projectively indigent* (*p-indigent*). While we do not know if *sp-poor* modules exist over every ring, their existence is determined for various families. For example, we determine that artinian serial rings have *sp-poor* modules. This work is a natural continuation to recent papers that have embraced the systematic study of the injectivity, projectivity and subinjectivity domains of rings. (This is a joint work with Sergio R. López-Permouth, Joseph Mastromatteo and José E. Simental-Rodríguez). (Received February 18, 2013)