

1119-13-234

Ashley K. Wheeler* (math@uark.edu), Department of Mathematical Sciences, SCEN 309, University of Arkansas, Fayetteville, AR 72701. *Principal minor ideals with matroid theory*. Preliminary report.

Let $K[X]$ denote the polynomial ring over an algebraically closed field K whose variables are entries in the generic $n \times n$ matrix X . Little is known about ideals \mathfrak{B}_t given by the size t principal minors of X : \mathfrak{B}_2 is a prime, normal complete intersection; \mathfrak{B}_{n-1} has two minimal primes, one is the determinantal ideal $I_{n-1}(X)$ and the other is given by the Zariski closure of the set of rank n matrices whose size $n - 1$ principal minors vanish.

This suggests a strategy for studying \mathfrak{B}_t in general, namely by studying the locally closed sets of rank r matrices whose size t principal minors vanish. In the case where $r = t$, the problem reduces to studying pairs of closed sets in a Grassmannian. We show that if a subset of Plücker coordinates for $\text{Grass}(n - 2, n)$ defines an irreducible algebraic set, then it is a positroid variety. It follows by a 2014 result of Knutson, Lam, and Speyer that the Zariski closure of the set of rank t matrices whose size t principal minors vanish is normal, Cohen-Macaulay, and has rational singularities. (Received February 16, 2016)