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**Lesley A. Ward\*** ([lesley.ward@unisa.edu.au](mailto:lesley.ward@unisa.edu.au)), School of Info Tech & Math Sci, University of South Australia, Mawson Lakes, SA 5095, Australia. *Product Hardy spaces associated to operators with heat kernel bounds on spaces of homogeneous type.*

Much effort has been devoted to generalizing the Calderón–Zygmund theory from Euclidean spaces to metric measure spaces, or spaces of homogeneous type. Here the underlying space  $\mathbb{R}^n$  with Euclidean metric and Lebesgue measure is replaced by a set  $X$  with general metric or quasi-metric and a doubling measure. Further, one can replace the Laplacian operator that underpins the Calderón–Zygmund theory by more general operators  $L$  satisfying heat kernel estimates.

I will present recent joint work with P. Chen, X.T. Duong, J. Li and L.X. Yan along these lines. We develop the theory of product Hardy spaces  $H_{L_1, L_2}^p(X_1 \times X_2)$ , for  $1 \leq p < \infty$ , defined on products of spaces of homogeneous type, and associated to operators  $L_1, L_2$  satisfying Davis–Gaffney estimates. This theory includes definitions of Hardy spaces via appropriate square functions, an atomic Hardy space, a Calderón–Zygmund decomposition, interpolation theorems, and the boundedness of a class of Marcinkiewicz-type spectral multiplier operators. (Received August 07, 2016)