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Janna Lierl* (janna.lierl@uconn.edu), Dept. of Mathematics, 341 Mansfield Road, Unit 1009, Storrs, CT 06269-1009. *Boundary Harnack principle and Dirichlet heat kernel estimates for nonsymmetric stable-like operators*. Preliminary report.

Consider the α -stable like operator

$$\Delta^{\frac{\alpha}{2}, \kappa} u(x) := \mathcal{A}(d, -\alpha) \lim_{\epsilon \rightarrow 0} \int_{\{y \in \mathbb{R}^d : |x-y| > \epsilon\}} \frac{\kappa(x, y)(u(y) - u(x))}{|x - y|^{d+\alpha}} dy, \quad x \in \mathbb{R}^d,$$

where $d \geq 2$, $\alpha \in (0, 2)$.

The existence of the heat kernel for this operator, as well as two-sided heat kernel estimates, have been proved in a recent work by Z.-Q. Chen and X. Zhang, under mild assumptions on κ . Namely, it suffices that κ is bounded between two positive constants, satisfies $\kappa(x, x+z) = \kappa(x, x-z)$ for all $x, z \in \mathbb{R}^d$, and $x \mapsto \kappa(x, x+z)$ is Hölder continuous of order β for some $\beta \in (0, 1)$.

Under somewhat stronger assumptions on κ , I will show a boundary Harnack principle with explicit decay rate $\delta(x)^{\alpha/2}$ on bounded $C^{1,1}$ -open sets in \mathbb{R}^d , where $\delta(\cdot)$ denotes distance to the boundary. Moreover, I will present two-sided estimates for the Dirichlet heat kernel on $C^{1,1}$ -open sets. (Received August 29, 2016)