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Panki Kim and **Renming Song*** (rsong@illinois.edu), Department of Mathematics,
University of Illinois at Urbana-Champaign, Urbana, IL 61801, and **Zoran Vondracek**. *Heat
kernels of non-symmetric jump processes: beyond the stable case.*

Let J be the Lévy density of a symmetric Lévy process in \mathbb{R}^d with its Lévy exponent satisfying a weak lower scaling condition at infinity. Consider the non-symmetric and non-local operator

$$\mathcal{L}^\kappa f(x) := \lim_{\epsilon \downarrow 0} \int_{\{z \in \mathbb{R}^d: |z| > \epsilon\}} (f(x+z) - f(z)) \kappa(x, z) J(z) dz,$$

where $\kappa(x, z)$ is a Borel measurable function on $\mathbb{R}^d \times \mathbb{R}^d$ satisfying $0 < \kappa_0 \leq \kappa(x, z) \leq \kappa_1$, $\kappa(x, z) = \kappa(x, -z)$ and $|\kappa(x, z) - \kappa(y, z)| \leq \kappa_2 |x - y|^\beta$ for some $\beta \in (0, 1)$. We construct the heat kernel $p^\kappa(t, x, y)$ of \mathcal{L}^κ , establish its upper bound as well as its fractional derivative and gradient estimates. Under an additional weak upper scaling condition at infinity, we also establish a lower bound for the heat kernel p^κ . (Received August 15, 2016)