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([p.e.shafer@leeds.ac.uk](mailto:p.e.shafer@leeds.ac.uk)), School of Mathematics, University of Leeds, Leeds, LS2 9JT, United Kingdom, and **Alexandra Soskova and Stefan Vatev**. *Cohesive powers of linear orders*.

A cohesive power of a computable structure is an effective analog of an ultrapower where a cohesive set acts as an ultrafilter. We study cohesive powers of computable copies of  $\omega$ , which are computable linear orders that are isomorphic to  $(\mathbb{N}, <)$ , but not necessarily by computable isomorphisms.

Every cohesive power of the standard presentation of  $\omega$  has order-type  $\omega + \zeta\eta$ , which is expected because  $\omega + \zeta\eta$  is the familiar order-type of countable non-standard models of PA. We show that it is possible for cohesive powers of computable copies of  $\omega$  to exhibit a variety of order-types:

- There is a computable copy of  $\omega$  with a cohesive power of order-type  $\omega + \eta$ .
- For every finite, non-empty  $X \subseteq \mathbb{N} \setminus \{0\}$  (thought of as a set of finite order-types), there is a computable copy of  $\omega$  with a cohesive power of order-type  $\omega + \sigma(X)$ . Here  $\sigma$  denotes the shuffle operation.
- For every  $X \subseteq \mathbb{N} \setminus \{0\}$  that is either  $\Sigma_2^0$  or  $\Pi_2^0$ , there is a computable copy of  $\omega$  with a cohesive power of order-type  $\omega + \sigma(X \cup \{\omega + \zeta\eta + \omega^*\})$ .

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