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Partial-Tuality Polynomials, Part 1.

The compositions of Poincaré duality ($*$) and Petrie duality (\times) yield a group of operators on maps that include Wilson duality ($*\times*$) and two triality operators ($*\times$ and $\times*$) that are inverses of each other. Ellis-Monaghan and Moffatt have generalized Chmutov's partial Poincaré duality construction for ribbon graphs to the other operators in this group, for which they coined the term *tualities*. The present authors have previously introduced the *partial- $*$ Euler-genus polynomial* that enumerates all the partial- $*$ duals according to Euler-genus. Here we introduce the partial- \bullet polynomials for the other four tualities. Part 1 of this two-part presentation focuses on the effect of the various partial tualities on the monodromy and on how the Euler-genus of a ribbon graph is easily determined directly from the monodromy. We present the symmetric embedding of $K_5 \rightarrow S_1$ as a counterexample to our conjecture in a predecessor paper that all partial- $*$ polynomials are log-concave. (Received September 07, 2020)