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**Austin Antonoiu, Ranthony A.C. Edmonds\*** (edmonds.110@osu.edu), **Bethany Kubik, Christopher O’Neill** and **Shannon Talbott**. *On Atomic Density of Numerical Semigroup Algebras*.

A numerical semigroup  $S$  is a cofinite, additively-closed subset of the nonnegative integers that contains 0. In this paper, we initiate the study of atomic density, an asymptotic measure of the proportion of irreducible elements in a given ring or semigroup, for semigroup algebras. For a fixed field  $\mathbb{F}$  and a numerical semigroup  $S$ , the numerical semigroup algebra  $\mathbb{F}[S]$  is the subring of  $\mathbb{F}[x]$  consisting only of terms of the form  $x^a$  for  $a \in S$ .

It is known that the atomic density of the polynomial ring  $\mathbb{F}_q[x]$  is zero for any finite field  $\mathbb{F}_q$ . We prove that the numerical semigroup algebra  $\mathbb{F}_q[S]$  also has atomic density zero for any numerical semigroup  $S$ . We also examine the particular algebra  $\mathbb{F}_2[x^2, x^3]$  in more detail, providing a bound on the rate of convergence of the atomic density as well as a counting formula for irreducible polynomials using Möbius inversion, comparable to the formula for irreducible polynomials over a finite field  $\mathbb{F}_q$ . (Received September 15, 2020)