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Gyu Whan Chang* (whan@inu.ac.kr), Incheon, 22012, South Korea, and **Jun Seok Oh**, Incheon, 22012. *The monoid of regular elements in commutative rings with zero divisors*. Preliminary report.

Let R be a commutative ring with identity, R^\bullet be the multiplicative monoid of regular elements in R , t be the so-called t -operation on R or R^\bullet . A Marot ring is a ring whose regular ideals are generated by their regular elements. The Marot ring was introduced by J. Marot in 1969 and has been playing a key role in the study of rings with zero divisors. The notion of Marot rings can be extended to t -Marot rings such that Marot rings are t -Marot rings. In this talk, we study some ideal-theoretic relationships between a t -Marot ring R and R^\bullet . We first construct an example of t -Marot rings that are not Marot. This also serves as an example of rank-one DVRs of reg-dimension ≥ 2 . Let R be a t -Marot ring, $t\text{-spec}(A)$ be the set of prime t -ideals of A , and $Cl(A)$ be the class group of A for $A = R$ or R^\bullet . Then, among other things, we prove that the map $\varphi : t\text{-spec}(R) \rightarrow t\text{-spec}(R^\bullet)$ given by $\varphi(P) = P^\bullet$ is bijective; $Cl(R) = Cl(R^\bullet)$; R is a Krull ring if and only if R^\bullet is a Krull monoid; and R is a factorial ring if and only if R is a Krull ring with $Cl(R) = \{0\}$. (Received August 30, 2020)