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**Laura Cossu\***, Institute of Mathematics and Scientific, Computing, Heinrichstrasse 36/III, 8010  
Graz, Austria. *Idempotent factorizations of singular  $2 \times 2$  matrices over quadratic integer rings.*

Let  $D$  be the ring of integers of a quadratic number field  $\mathbb{Q}[\sqrt{d}]$ . Addressing the classical open problem of the characterization of integral domains  $R$  such that every singular (*i.e.*, with zero determinant) matrix over  $R$  is a product of idempotent matrices, we investigate the idempotent factorization of  $2 \times 2$  singular matrices over  $D$ . We show that when  $d < 0$  there exist singular matrices that do not admit an idempotent factorization, while in case  $d > 0$  we use Vaseršteĭn's result (1972) that  $SL_2(D)$  is generated by transvections to prove that any  $2 \times 2$  matrix with either a null row or a null column is a product of idempotents. As a consequence, every dimension 2 column-row matrix over a real quadratic integer ring decomposes into idempotent factors. Based on a joint work with P. Zanardo. (Received August 16, 2020)