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Shaun Cooper* (s.cooper@massey.ac.nz). *Some elliptic integrals in Ramanujan's lost notebook.*

In the “lost notebook” [2, p. 53] Ramanujan stated a result equivalent to

$$\int_0^x t f(-t) f(-t^5) t(-t^7) f(-t^{35}) dt = \int_0^v \frac{1}{\sqrt{\left(\frac{1}{t} + 1 - t\right) \left(\frac{1}{t^3} - \frac{5}{t^2} - 9 - 5t^2 - t^3\right)}} \frac{dt}{t}$$

where

$$f(-t) = \prod_{j=1}^{\infty} (1 - t^j)$$

and

$$v = x \frac{f(-x) f(-x^{35})}{f(-x^5) f(-x^7)}.$$

In this talk I will describe how this result fits into a larger theory, and indicate how to obtain the corresponding result involving $f(-t) f(-t^3) t(-t^7) f(-t^{21})$ which is new. This is joint work with T. Anusha, E.N. Bhuvan and K.R. Vasuki, [1].

References:

- [1] T. Anusha, E.N. Bhuvan, S. Cooper and K.R. Vasuki, *Elliptic integrals and Ramanujan-type series for $1/\pi$ associated with $\Gamma_0(N)$, where N is a product of two small primes*, J. Math. Anal. Appl., **472** (2019) 1551–1570.
- [2] S. Ramanujan, *The Lost Notebook and Other Unpublished Papers*, Narosa, New Delhi, 1988. (Received September 15, 2020)