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Calderon-Zygmund type estimates for nonlocal PDE with Holder continuous kernel.

In this talk I will present a result on L^p -regularity of weak solutions to linear nonlocal equation. To be precise, we study solutions of $\mathcal{L}_K^s u = f$ where the nonlocal operator is given by $\mathcal{L}_K^s u(x) = - \int_{\mathbb{R}^n} K(x, y) \frac{u(x) - u(y)}{|x - y|^{n+2s}} dy$. We prove that for $s \in (0, 1)$, $t \in [s, 2s]$, $p \in [2, \infty)$, K an elliptic, symmetric, and $K(\cdot, y)$ is *uniformly Hölder continuous*, the solution u belongs to $H_{loc}^{2s-t, p}(\Omega)$ as long as $2s - t < 1$ and $f \in \left\{ H_{loc}^{t, p'}(\mathbb{R}^d) \right\}^*$. The increase in differentiability and integrability is independent of the Hölder coefficient of K . For example, in the event that $f \in L_{loc}^p$, we can deduce that the solution $u \in H_{loc}^{2s-\delta, p}$ for any $\delta \in (0, s]$ as long as $2s - \delta < 1$. The proof uses a perturbation argument where regularity of solutions of a simpler equation is systematically used to obtain a desired estimate.

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