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*Periodic points of quadratic rational functions in towers of finite fields.* Preliminary report.

Let  $\mathbb{F}_q$  be a finite field with  $q$  elements and  $\phi$  a rational function with coefficients in  $\mathbb{F}_q$ . For each  $n \geq 1$ , the orbit of every  $x \in \mathbb{F}_{q^n}$  under  $\phi$  is either periodic or strictly preperiodic. Little is known about how the proportion of such  $x$  that are periodic changes as  $n$  grows. Part of what makes the problem difficult is that, since  $\phi$  is defined over a finite field, it is necessarily post-critically finite. We study the case where  $\phi$  is quadratic, and show that in all but a few special cases the  $\liminf$  of this proportion is zero. The proof begins by using the Chebotarev density theorem over function fields and a result of Pink on lifting to characteristic zero. But the real guts of it are group-theoretic and complex dynamical: we make a careful study of the iterated monodromy groups of post-critically finite quadratic rational functions over  $\mathbb{C}$ , including several new results about the fixed-point proportion of the natural action of these groups on the infinite rooted binary tree. (Received September 15, 2020)